

problem 4.

A CCD detector will be used for photometry of a galaxy with average surface brightness in Johnson's B band $B = 21.8 \text{ mag/arcsec}^2$.

Knowing that:

- All observations were performed in dark sky (new moon), with a sky brightness $B = 22.6 \text{ mag/arcsec}^2$.
- The CCD has a quantum efficiency of 87% at 4344 \AA , 0.2 arcsec square pixels and it is read at a frequency that provides a RON of $5 e^-$ (RMS). Consider a linear response regime, negligible dark counts and no contribution from illumination and flatfield corrections to the error budget.
- The observations were performed at a 7.7m effective diameter telescope. The optical path has an overall efficiency of 70% at 4344 \AA .
- A nearly constant airmass ($X=1.2$) can be assumed in addition to first order extinction with coefficient $K_B = 0.21 \text{ mag}$ for all exposures. Ignore the second order extinction coeffs.
- Consider that a constant sky brightness (in counts/pix/s) can be evaluated from the mode of many pixels values (over a large solid angle), yielding a well defined background value with negligible uncertainty when compared to the source photon noise.
- The standard Vega ($B=0.0$) flux outside the atmosphere ($X=0.0$) at 4344 \AA is $f_\lambda = 6.32 \times 10^{-9} \text{ erg cm}^{-2} \text{ s}^{-1} \text{ \AA}^{-1}$ (Bessel 1998).
- The effective central wavelength of B band are: $\lambda_{\text{eff}} = 4344 \text{ \AA}$; $\Delta\lambda_{\text{eff}} = 98 \text{ \AA}$.
- Four (4) 1200 s exposures where taken.

- i. Calculate the final S/R per pixel in the surface brightness for the combined (co-added) set of exposures.
- ii. Calculate the S/R per resolution element (FWHM) for an image quality of 1.0 arcsec (FWHM).
- iii. Find the fractional contribution to the total variance (σ^2) from
 - ii.1 sky background,
 - ii.2 readout noise and
 - ii.3 source photon counting.

Constants: $h = 6.626 \times 10^{-27} \text{ erg s}$; $c = 2.998 \times 10^{10} \text{ cm s}^{-1}$.