

# Fotometria III

## Extinção e Avermelhamento Interestelar

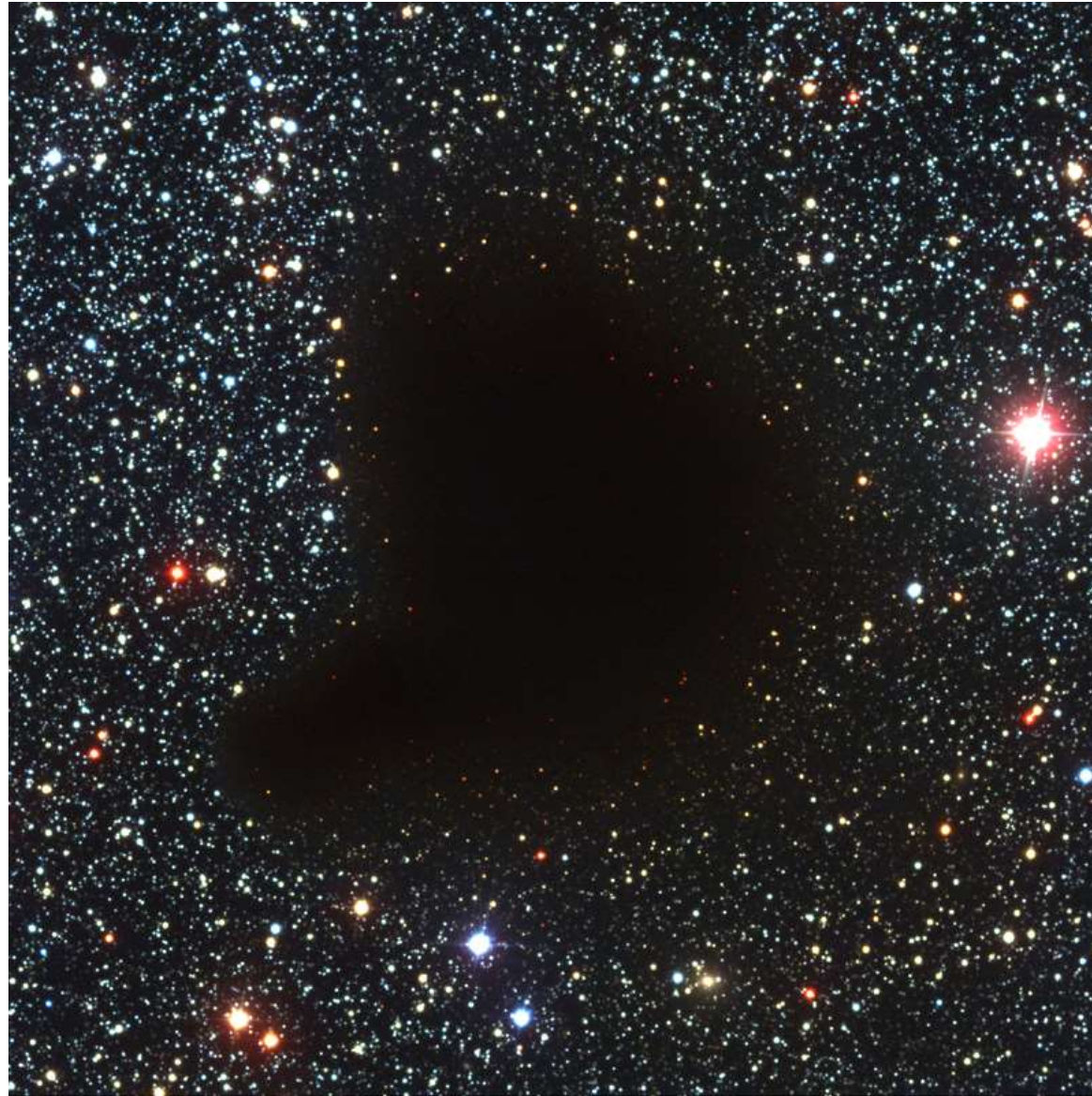


- O meio interestelar é composto de poeira (partes escuras e azuis) e gás (vermelho).





# Nuvens escuras de poeira



ESO PR Photo 20a/99 ( 30 April 1999 )

The "Black Cloud" B68  
(VLT ANTU + FORS1)

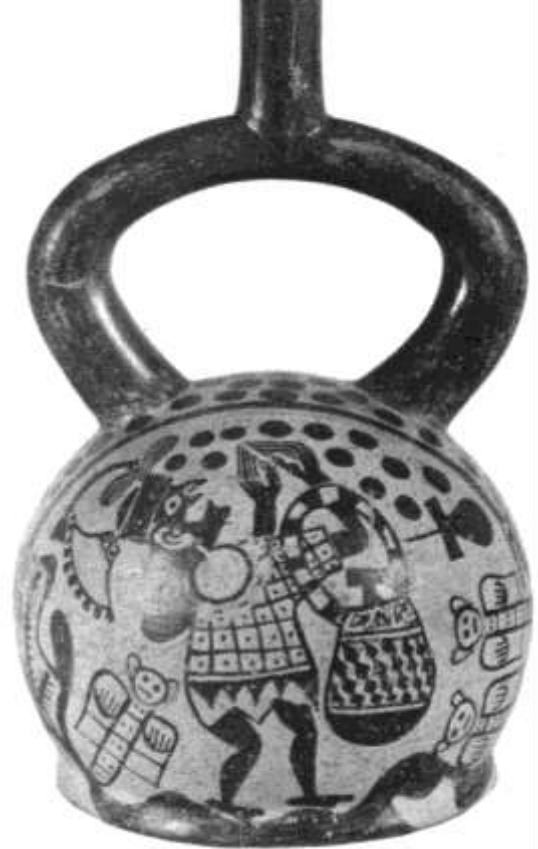
© European Southern Observatory 

# Primeiras observações do meio interestelar



Civilizações europeias apenas reconheceram constelações brilhantes (estrelas)

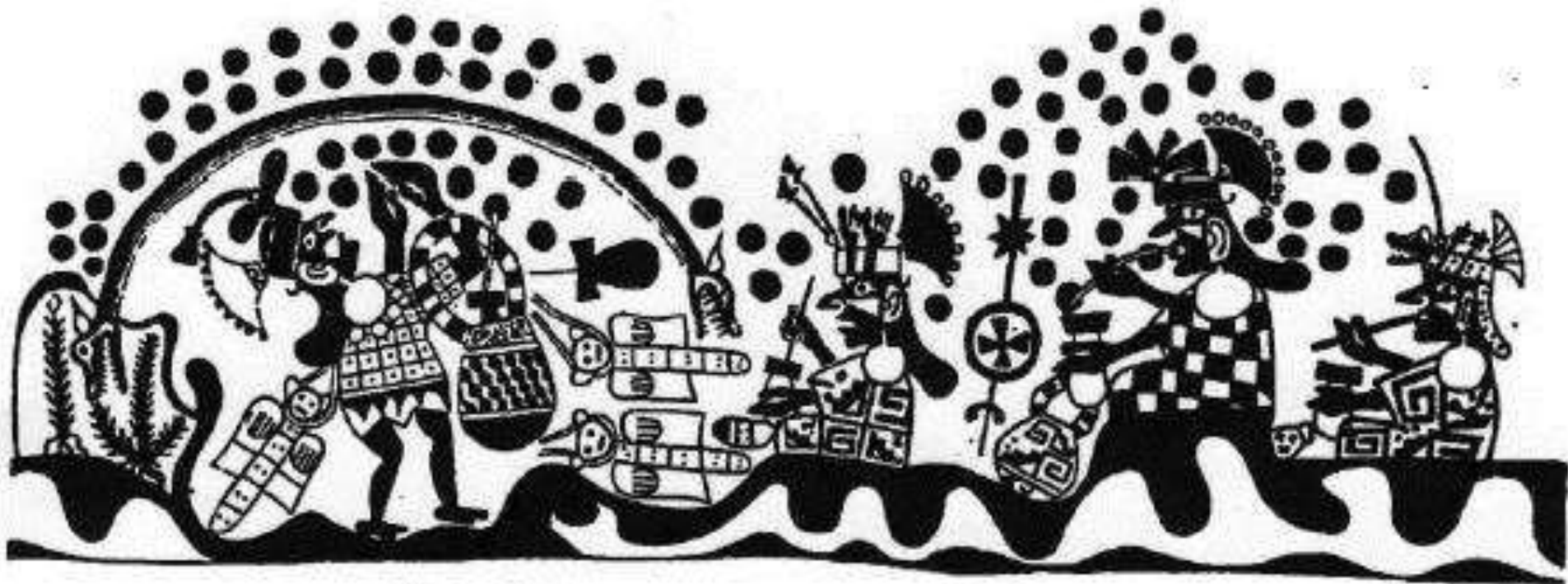




Inca  
empire

No hemisfério Sul foram  
reconhecidas constelações escuras

Civilizações andinas  
(2000a.C. – 1542)  
identificaram  
constelações escuras



Civilizações andinas observaram em detalhe a via láctea (= mayu, ou rio celestial)

Foto: Fred Espenak

*Cronista espanhol: “No hablo sólo de las partes lúcidas y resplandecientes ... sino digo esto por otras partes oscuras y negras que hay en el cielo ... las cuales jamás me acuerdo de haber echado de ver en el cielo cuando estaba en Europa, y acá, en este otro hemisferio, las he visto muy manifiestas ”*  
*José Acosta [1590]*



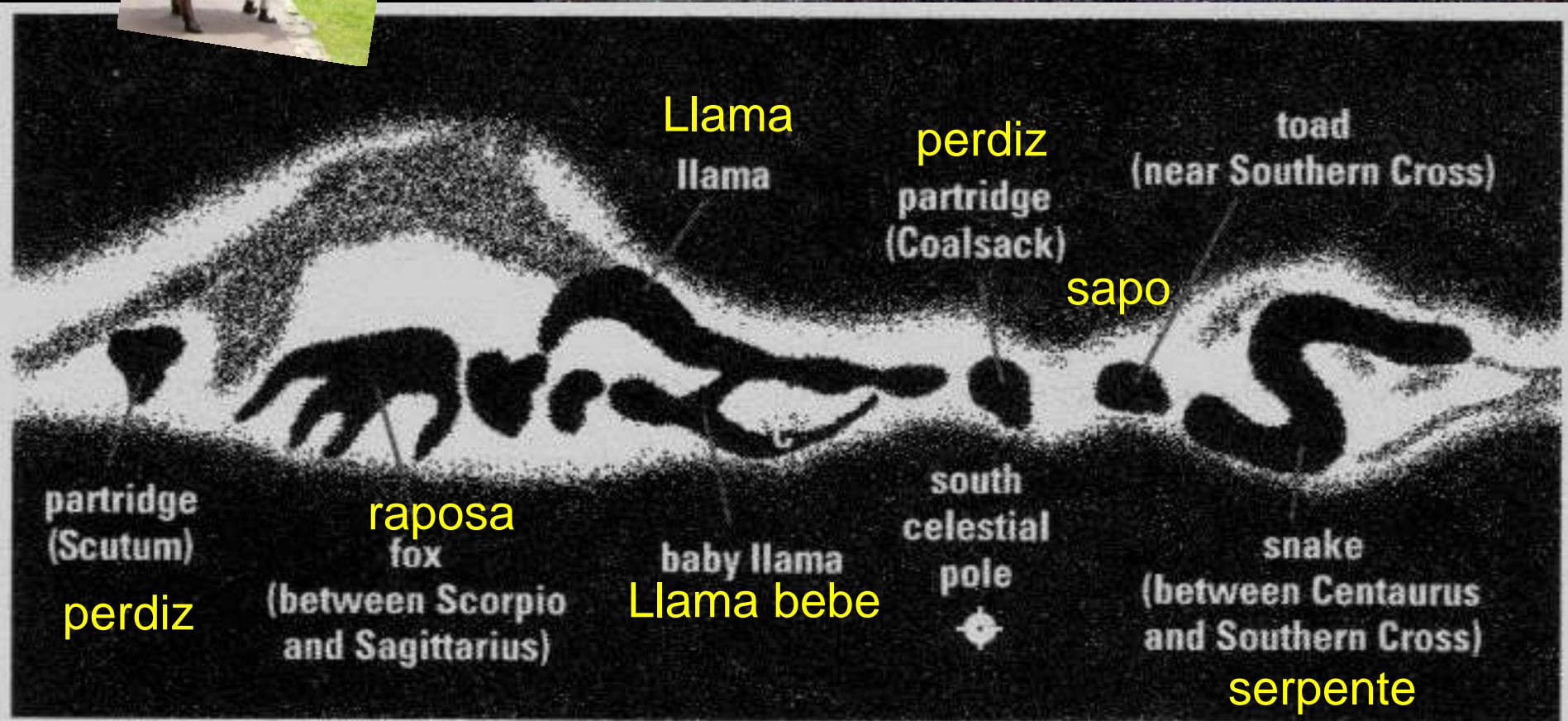
# Constelação escura da Llama: Yacana



*$\alpha$ ,  $\beta$  Centauri:  
Llama Ñahui:  
Olhos da Llama*



# Constelação escura da Llama: Yacana



(c)

**Figure 2.15** (Continued). (c) Contemporary Andean dark cloud constellations of the southern Milky Way; to the people of Misminay, dark cloud constellations represent animals.

Aveni,  
Stairways  
to the  
Stars,  
1997

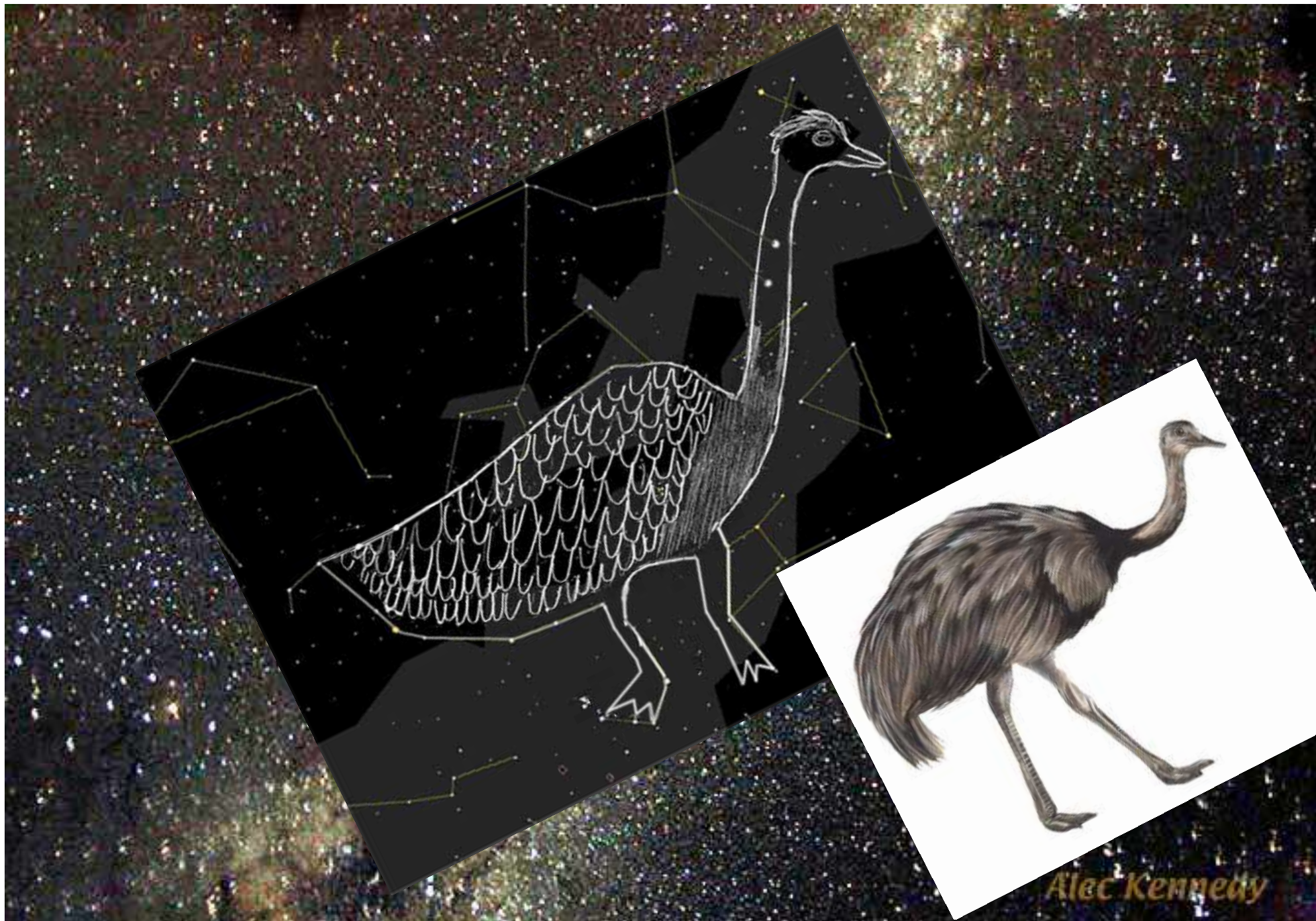




Austrália:  
Emu



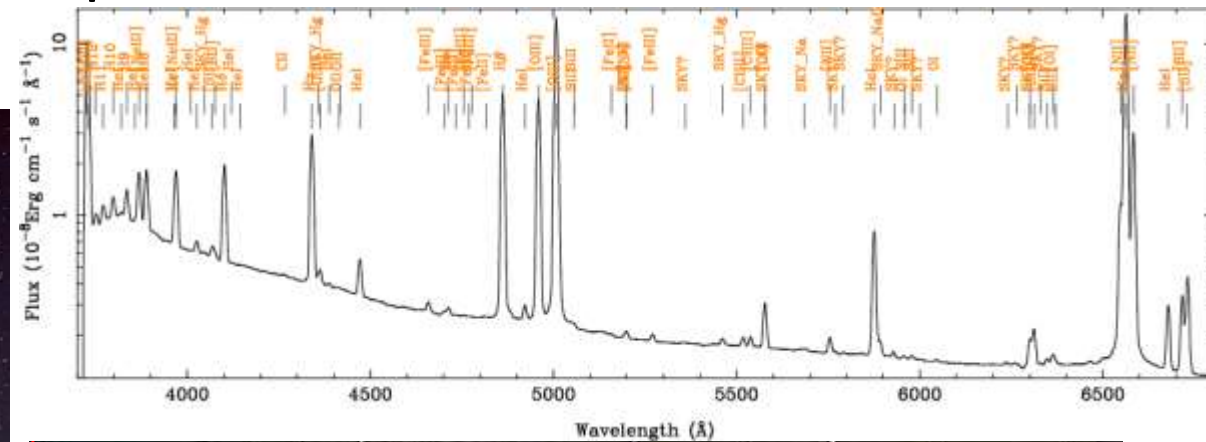
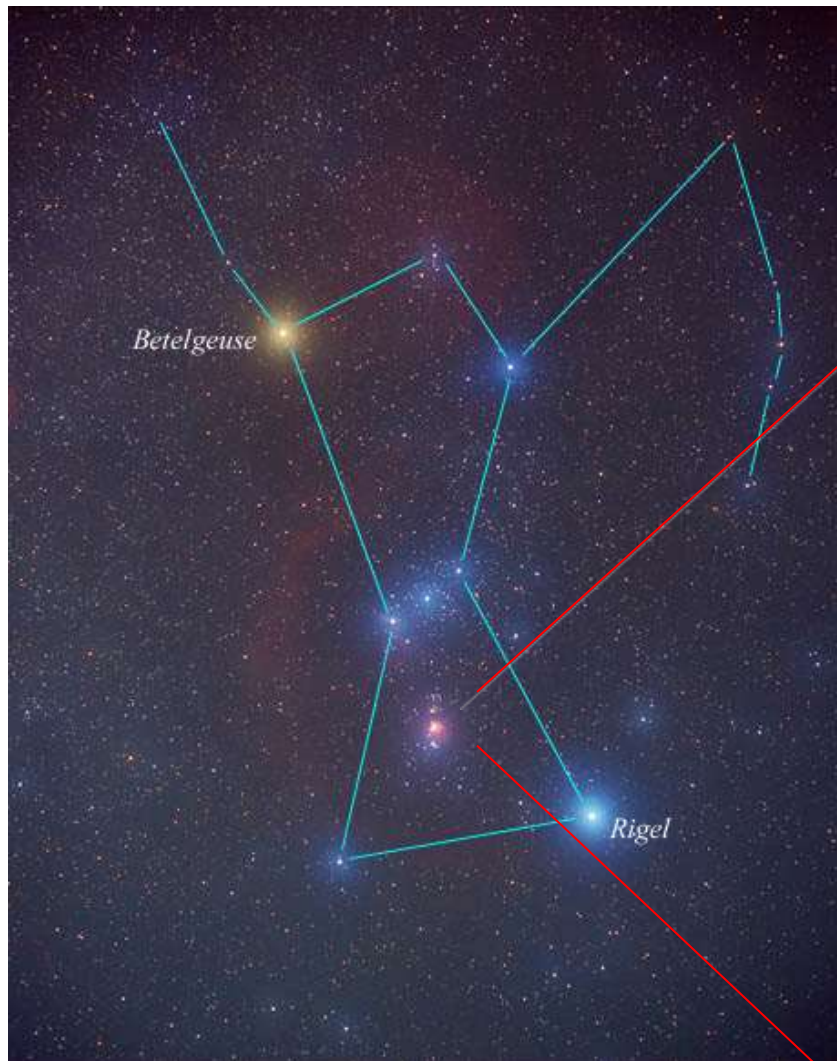
# Brasil: Ema





# A finais do século XIX e começos do século XX a existencia do meio interestelar foi confirmada

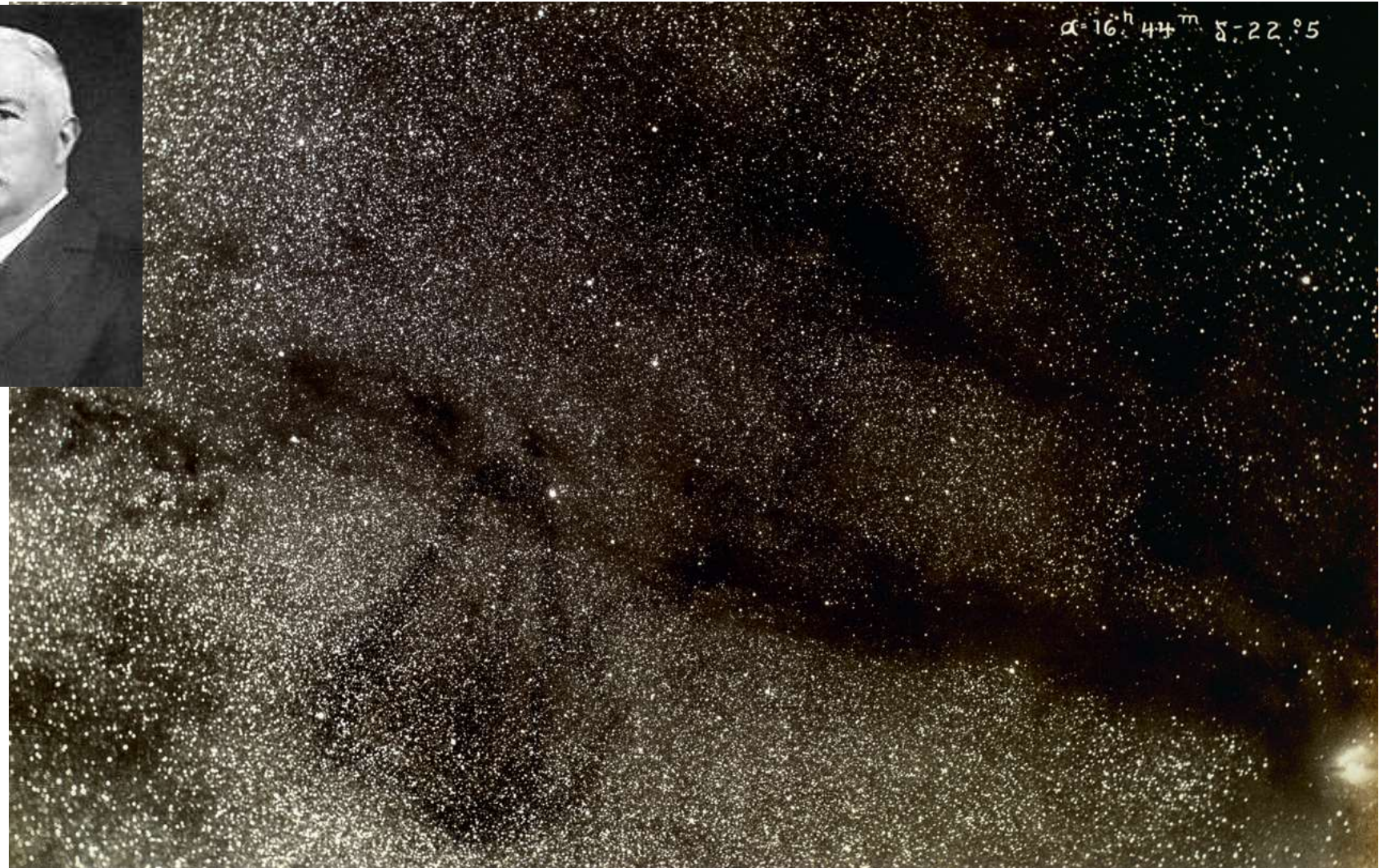
Huggins & Miller (1863) observaram o espectro da nebulosa de Órion e encontraram que o espectro de emissão era característico de gás.





## A finais do século XIX e começos do século XX a existencia do meio interestelar foi confirmada

**Edward Emerson Barnard** (1857 – 1923) produced in 1895 the first images of dark nebulae and came to the conclusion that along with the illuminated gas and dust there was also significant quantities of dust and gas not directly illuminated.



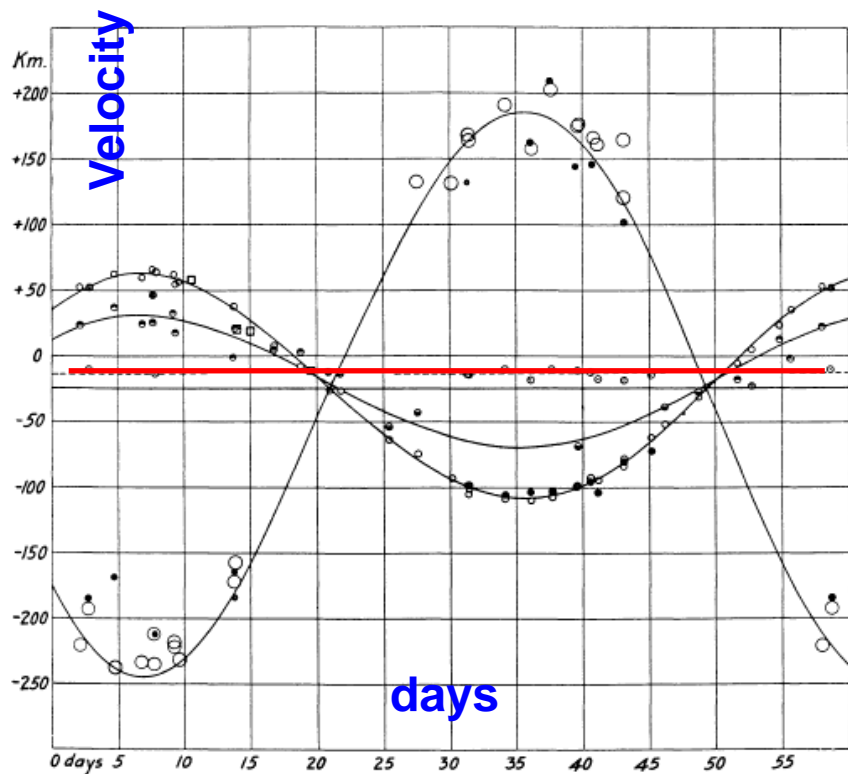


# Linhas interestelares estacionárias in the spectra of spectroscopic binaries

Hartmann (1904)

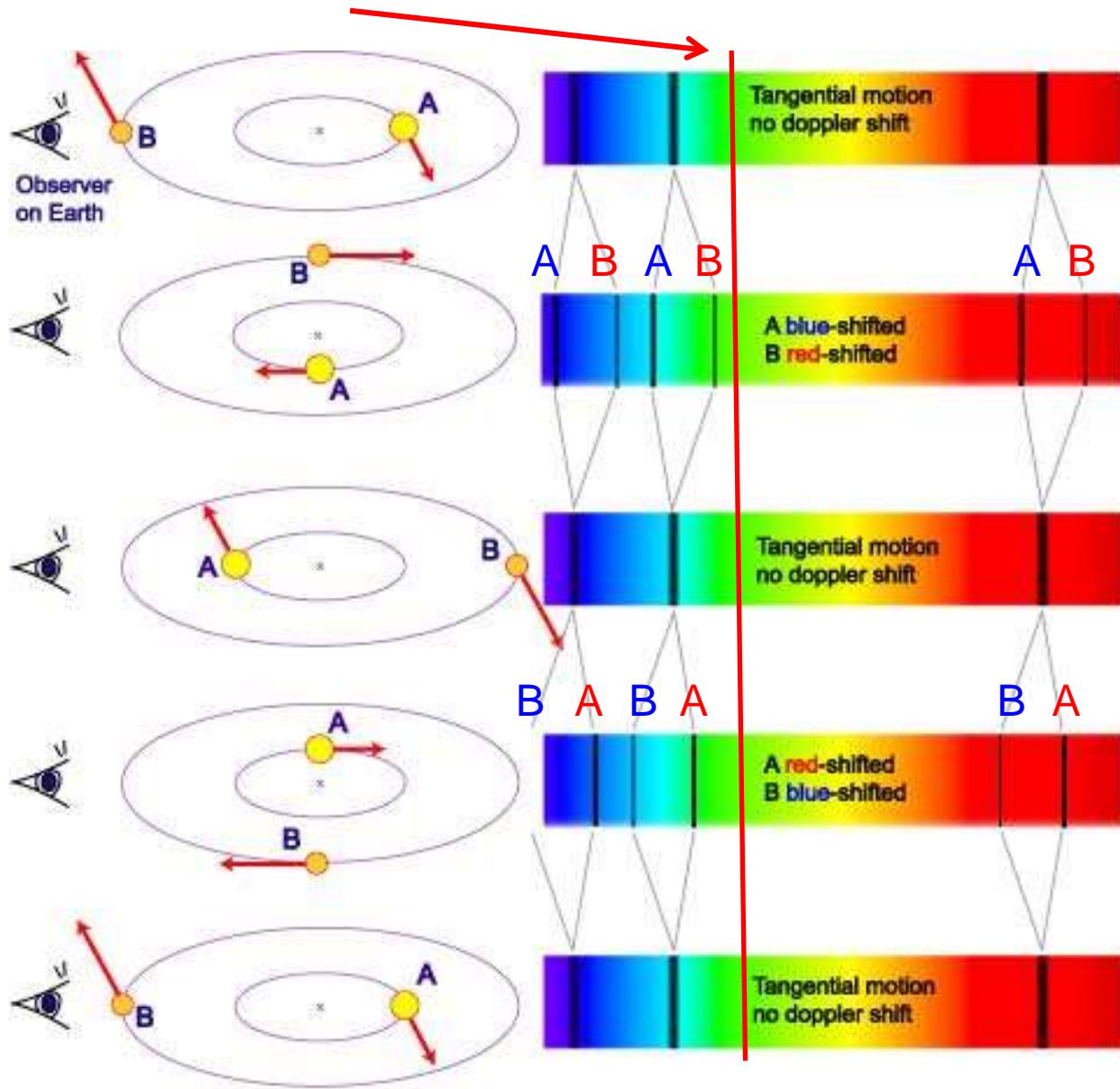
Heger (1918)

J. A. Pearce (1932)



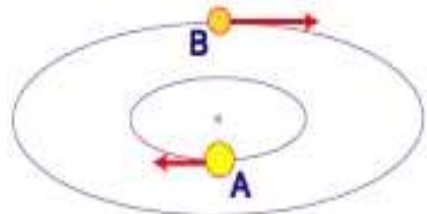
Primary stellar.....○  
 Secondary stellar.....○  
 Stellar calcium.....●  
 Inter-stellar calcium.....○  
 Blended calcium.....□  
 Mt. Wilson.....□

Radial Velocity Curves of H.D. 698



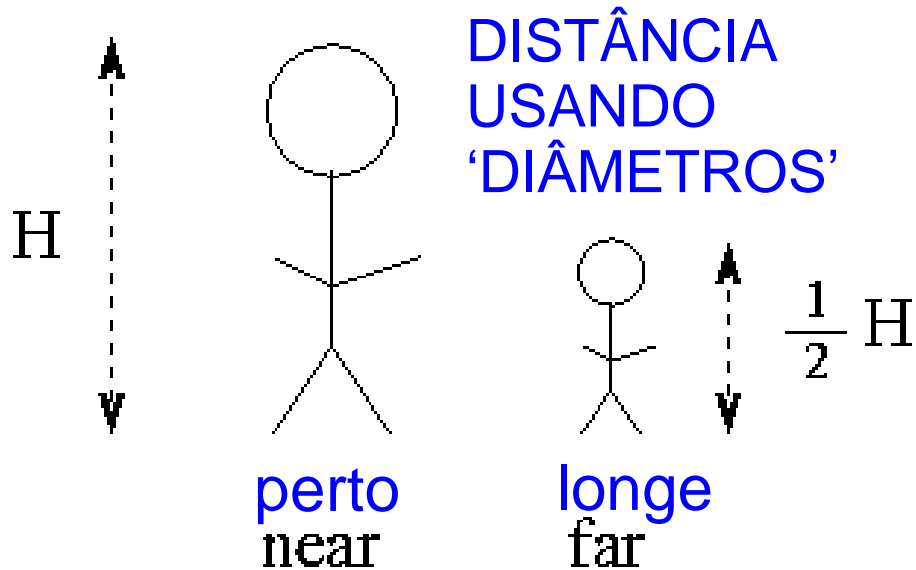
## A Spectroscopic Binary System

High-mass star A and lower-mass B orbit around a common centre of mass. The observed combined spectrum shows periodic splitting and shifting of spectral lines. The amount of shift is a function of the alignment of the system relative to us and the orbital speed of the stars.

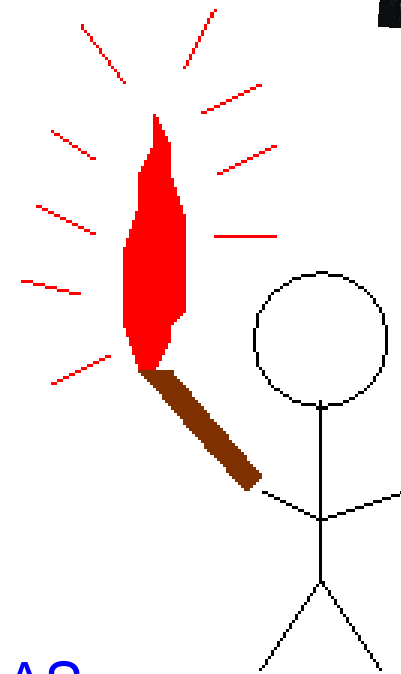


In 1930, Robert Trumpler estimated distances of about 100 open star clusters by measuring:

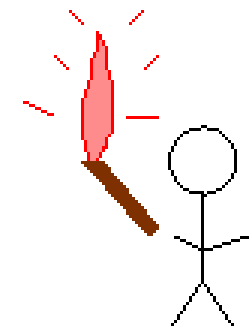
- angular size of the cluster
- central concentration and # of stars
- brightness & spectral class of stars in the OC



**DISTÂNCIAS FOTOMETRICAS**



perto  
near

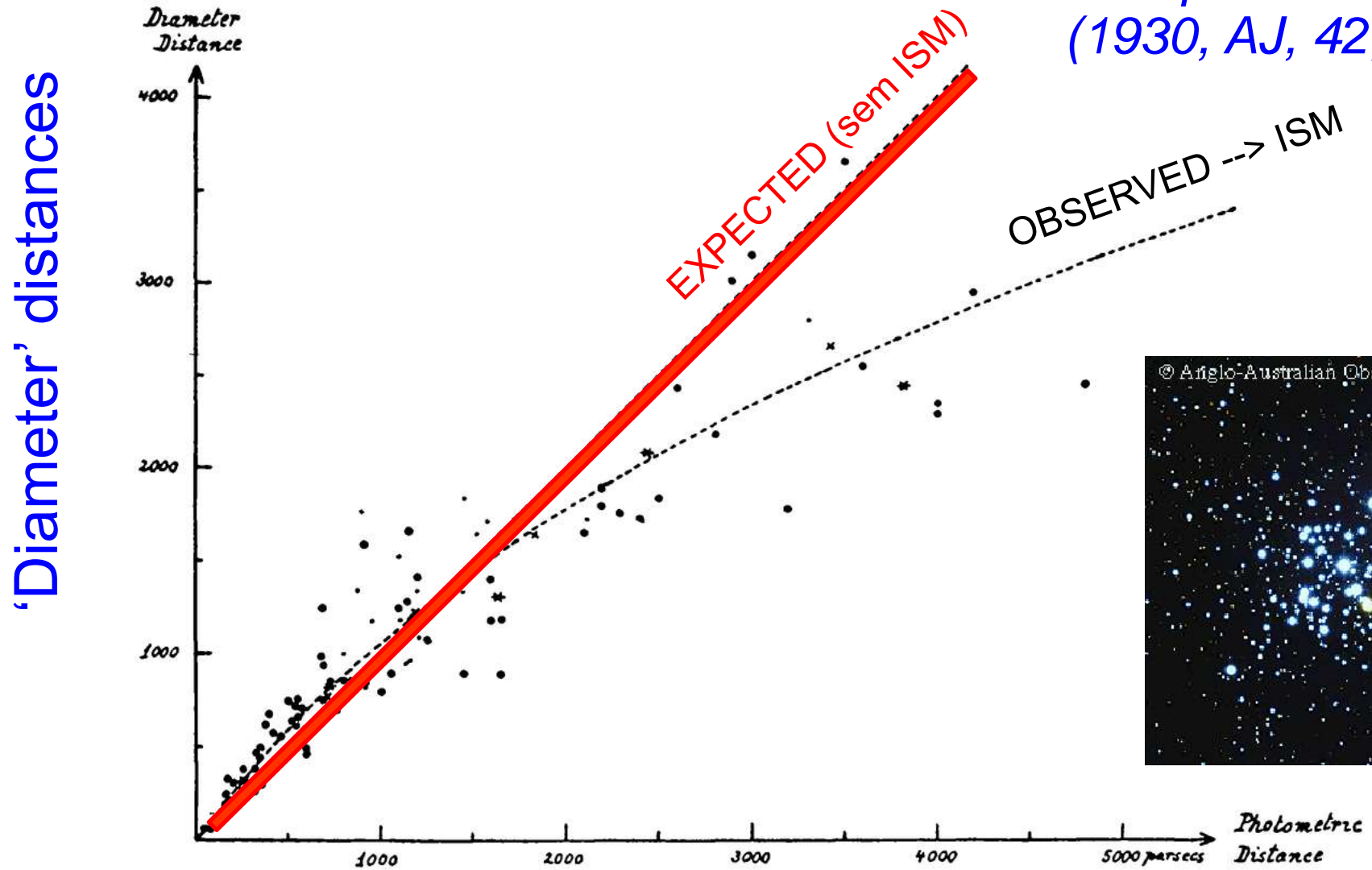


longe  
far



# Comparação entre distâncias baseadas em 'diâmetros' e em 'fotometria'

Trumpler  
(1930, AJ, 42, 214)



'Diameter' distances

'Photometric' distances



# Poeira: afeta a fotometria

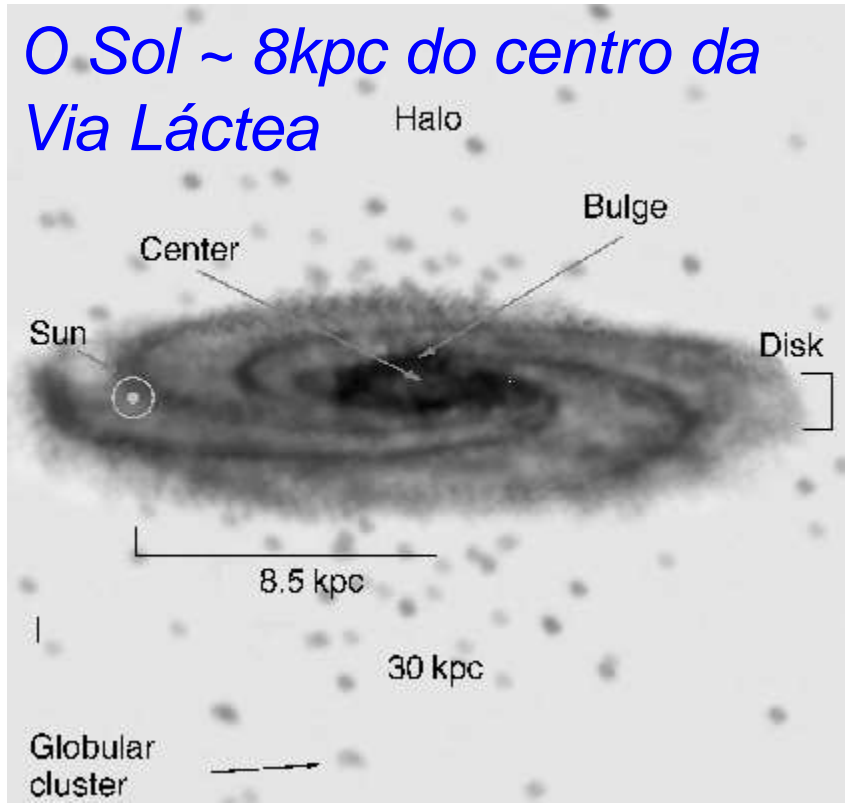
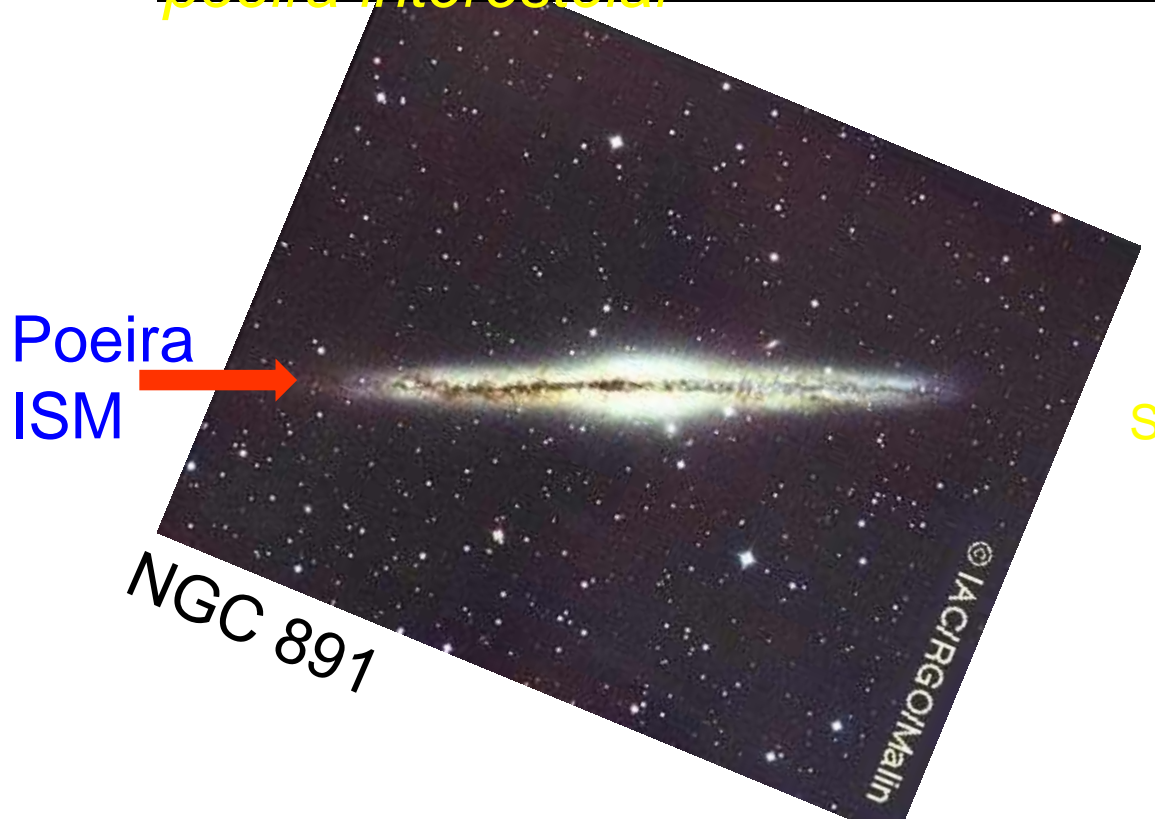
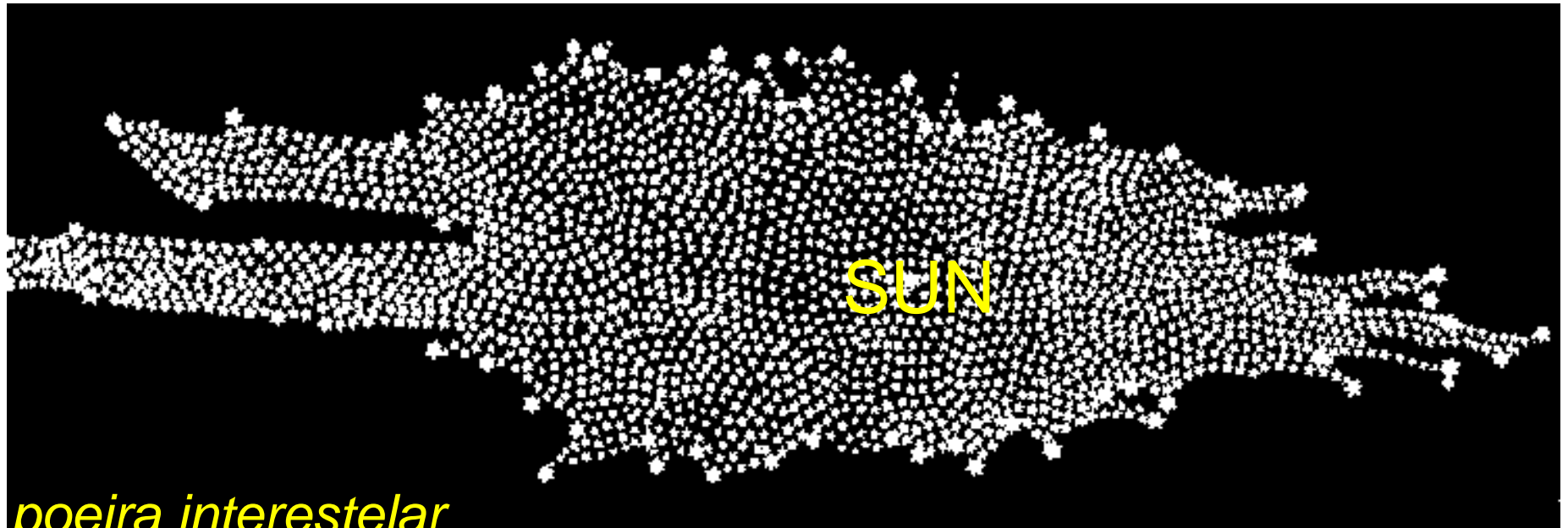
*Via Láctea no óptico*

A poeira bloqueia a luz das estrelas  
no disco da Via Láctea

*Via Láctea no infravermelho*



# A Galáxia de acordo ao William Herschel (1780s)



S

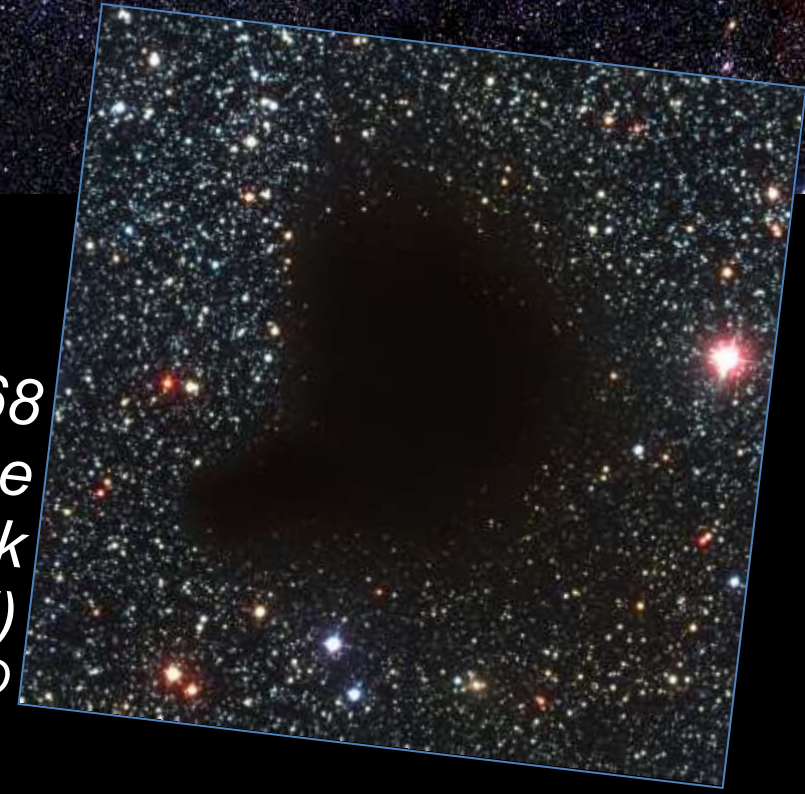


# Efeitos da poeira: extinção

*Via Láctea no óptico*

A atenuação da luz das  
estrelas pela poeira  
interestelar chama-se  
**extinção**

*B68  
(the  
black  
cloud)  
ESO*





# Efeitos da poeira: avermelhamento

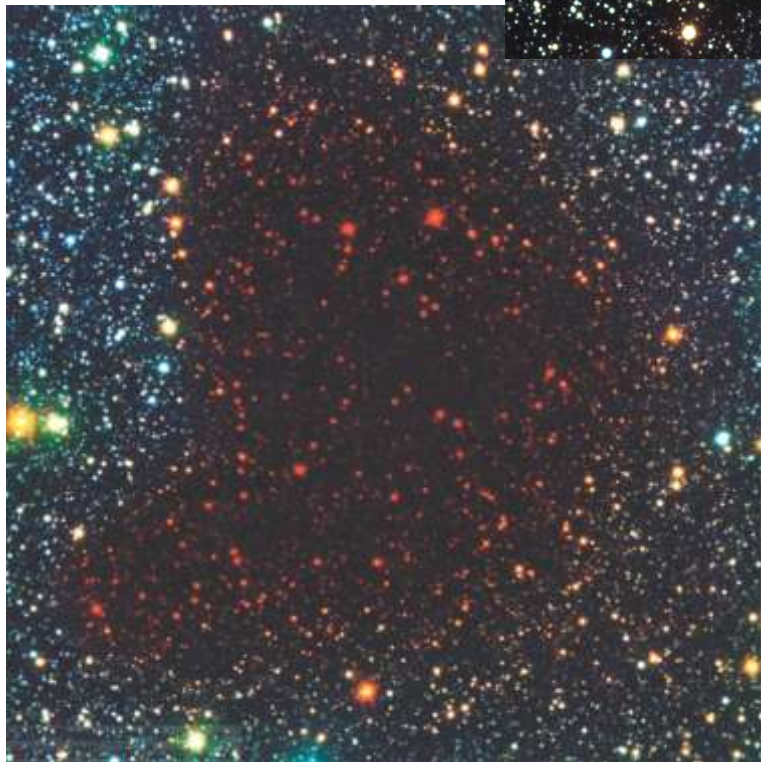
A poeira absorve  
mais a luz azul  
do que a  
vermelha,  
causando o  
chamado  
*reddening* ou  
avermelhamento





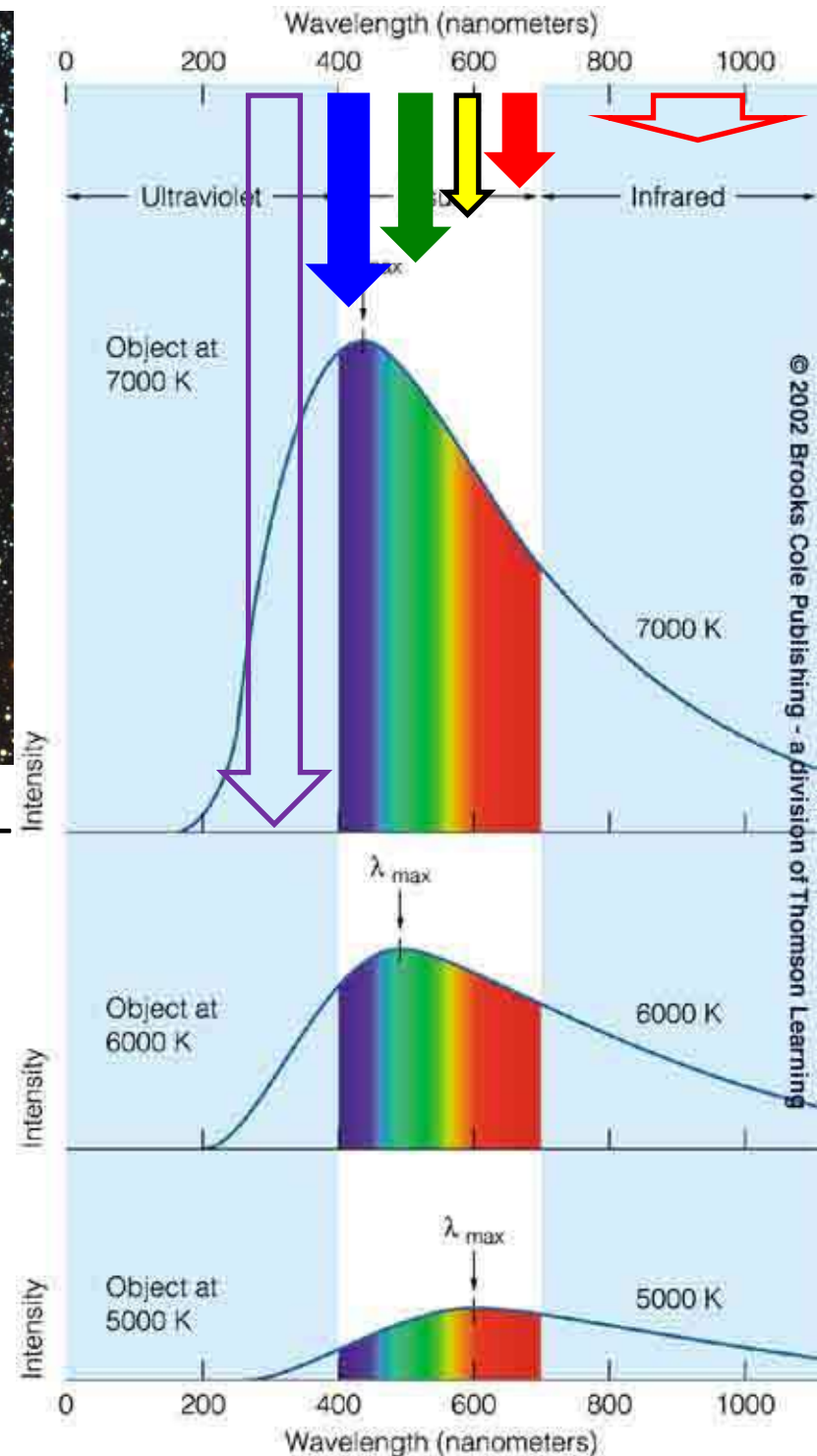
# Avermelhamento interestelar

Optical light is strongly scattered and absorbed by interstellar clouds



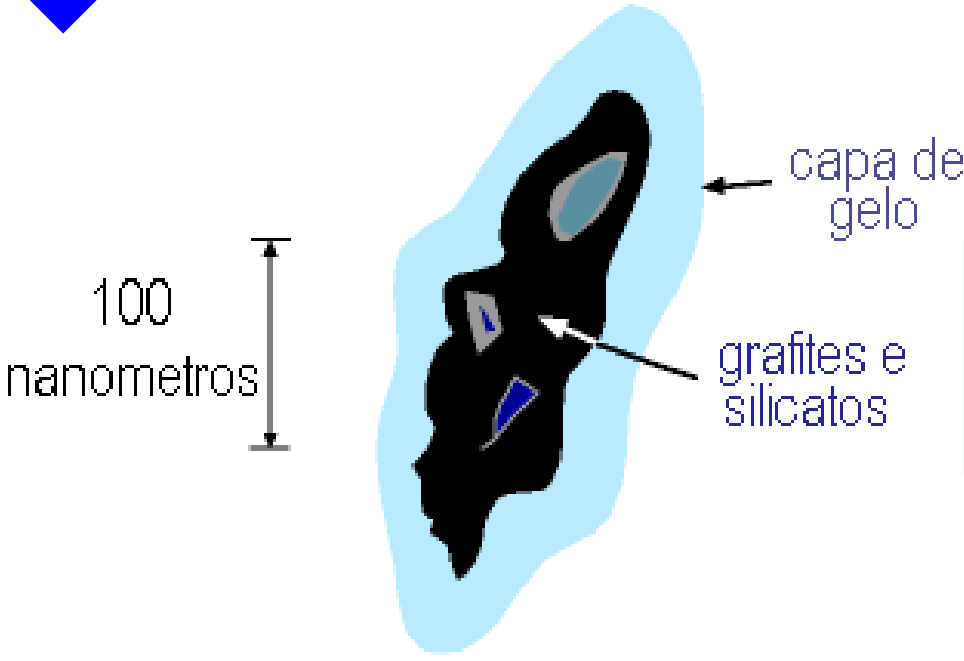
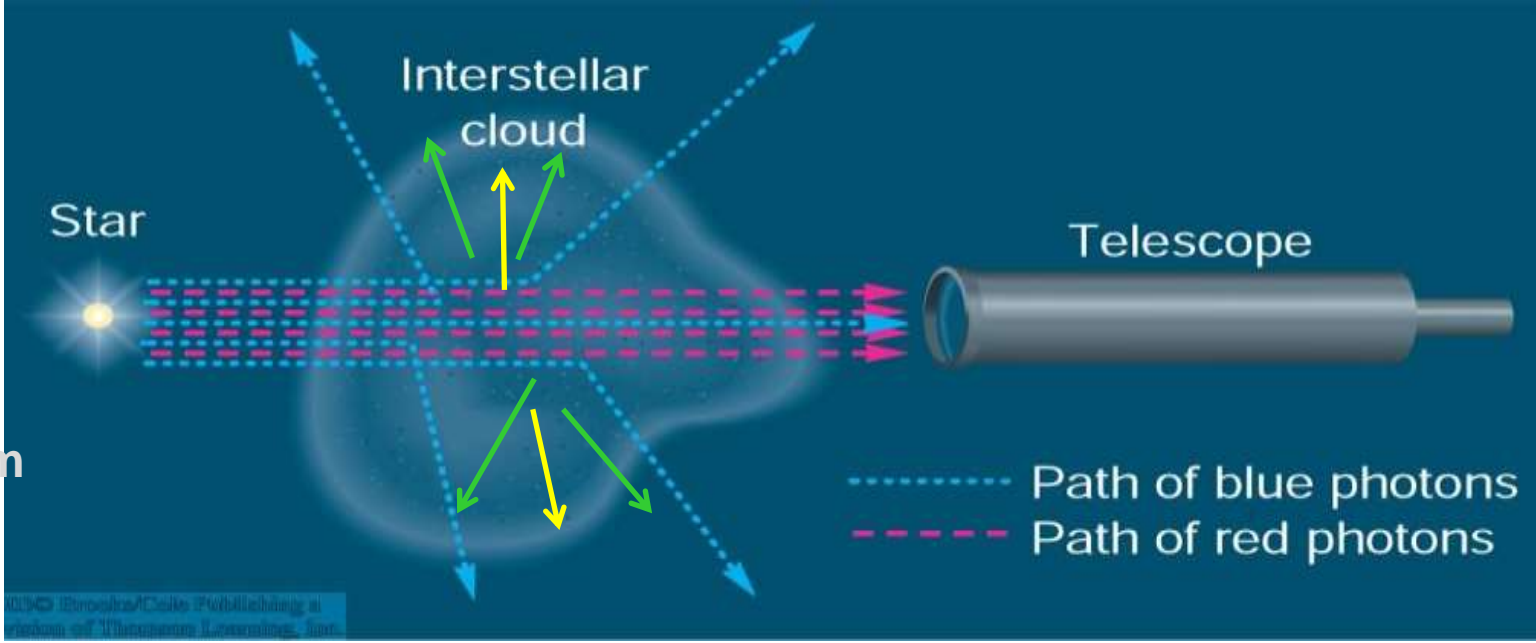
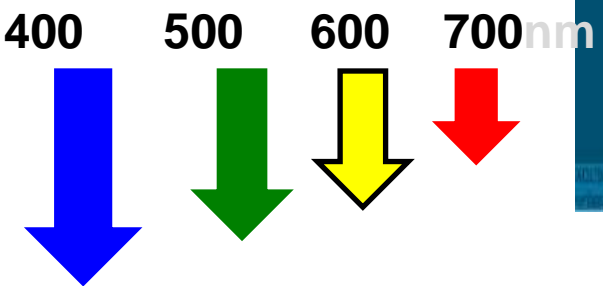
OPTICAL

INFRARED



# Extinção e avermelhamento por poeira

Luz de menor  $\lambda$  é mais espalhada e absorvida pela poeira



Grão de poeira

Probability of scattering  $\propto \frac{1}{\lambda}$



# Nebulosa de reflexão

A poeira espalha mais a luz azul

Probability of scattering  $\propto \frac{1}{\lambda}$



*Pleiades*



# Densidade da poeira IS

*Via Láctea no óptico*

Apenas  $10^{-6}$  partículas de poeira por  $\text{m}^3$   
ou 1000 por  $\text{km}^3$

Sendo tão pouco densa, como pode a poeira atenuar a luz vinda das estrelas?

Distância típica entre estrelas  $\sim 3.5$  a.l. =  $3.3 \times 10^{16}$  m



# A componente mais abundante do meio interestelar é o gás

Em média a densidade do meio interestelar é extremamente baixa: 1 átomo / m<sup>3</sup> ( 10<sup>6</sup> átomos / m<sup>3</sup>)

Regiões variam de 10<sup>4</sup> a 10<sup>9</sup> átomos/m<sup>3</sup>

Melhor vácuo conseguido em lab : 10<sup>10</sup> moléculas/m<sup>3</sup>

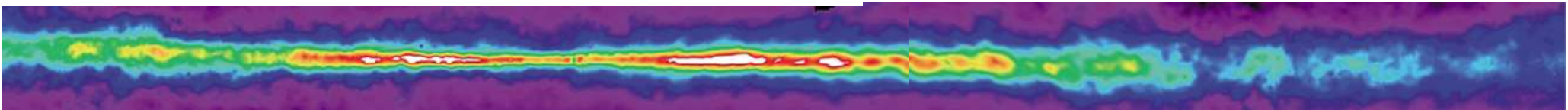
**VISIBLE LIGHT** (0.4–0.6 micron)

Reveals nearby stars and tenuous ionized gas; dark areas are cold and dense

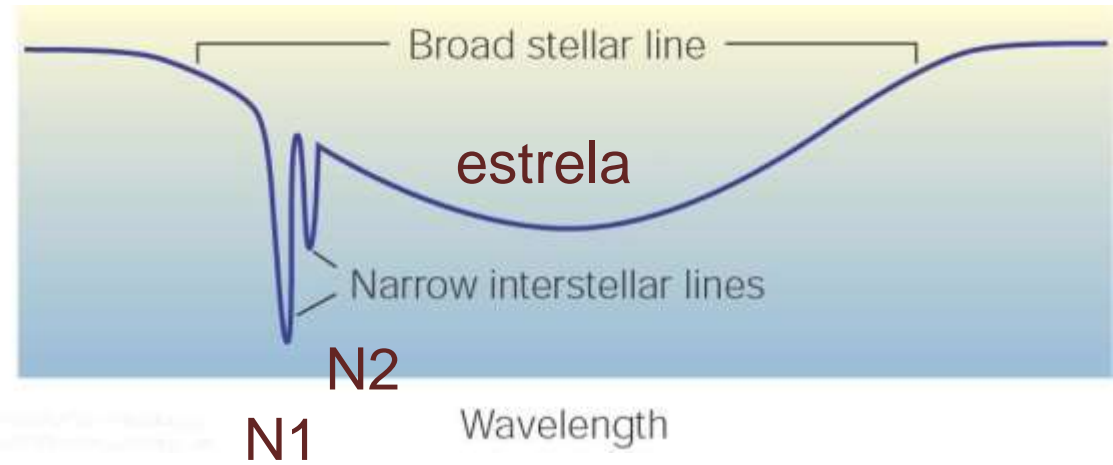
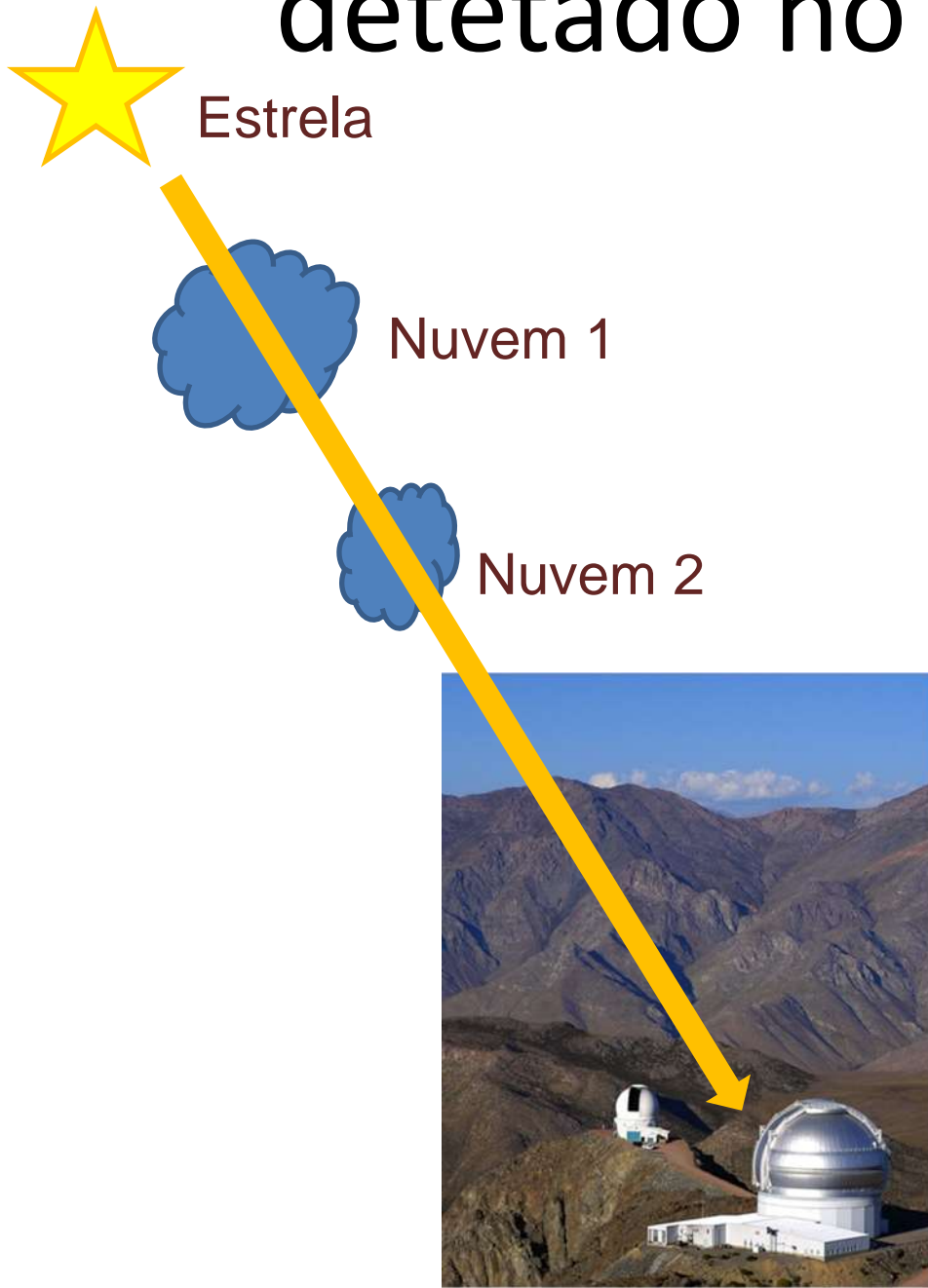


**ATOMIC HYDROGEN** (1420 MHz)

Reveals neutral atomic hydrogen in interstellar clouds and diffuse gas



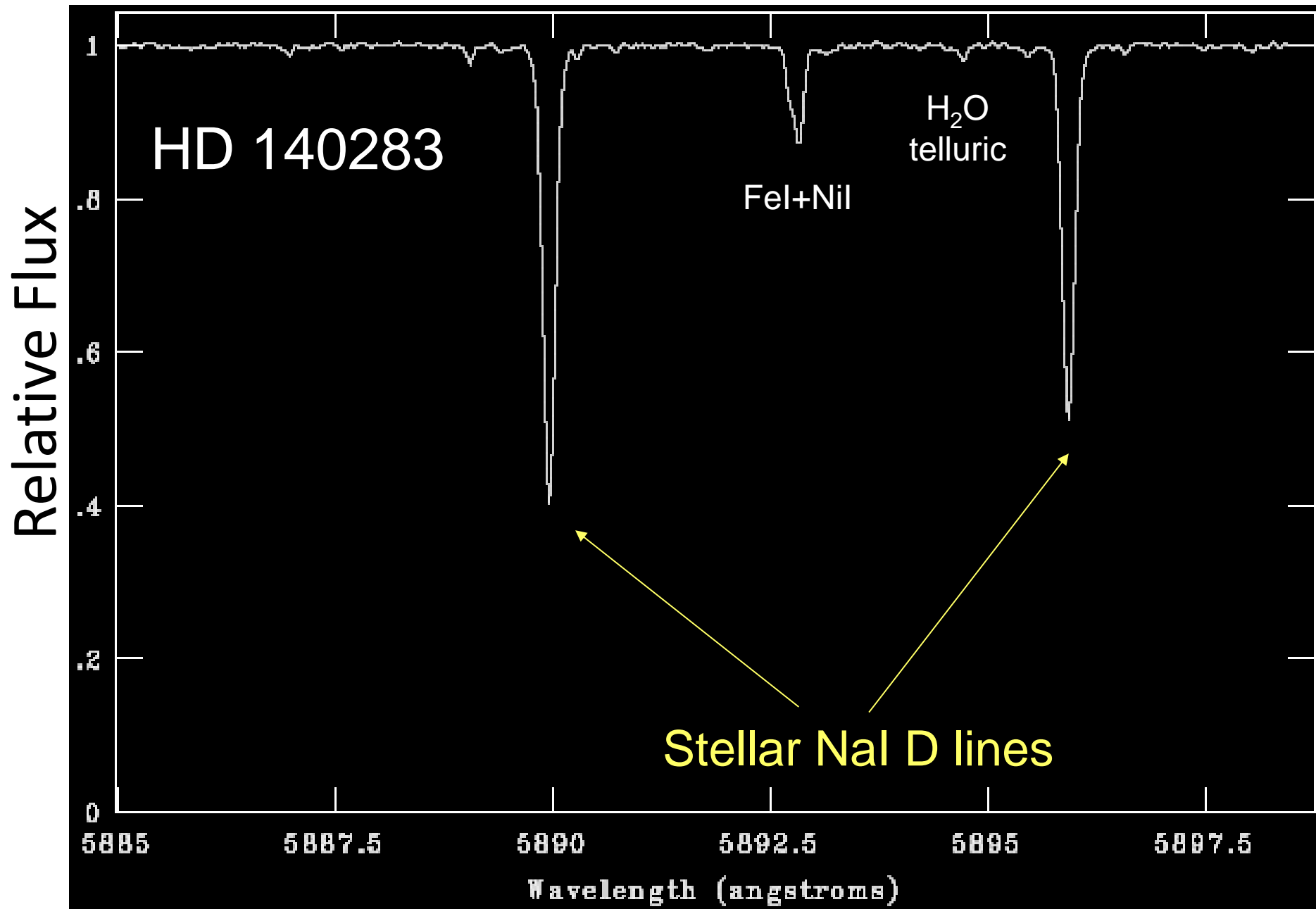
# Gás neutro tb é possível de ser detetado no espectro visível





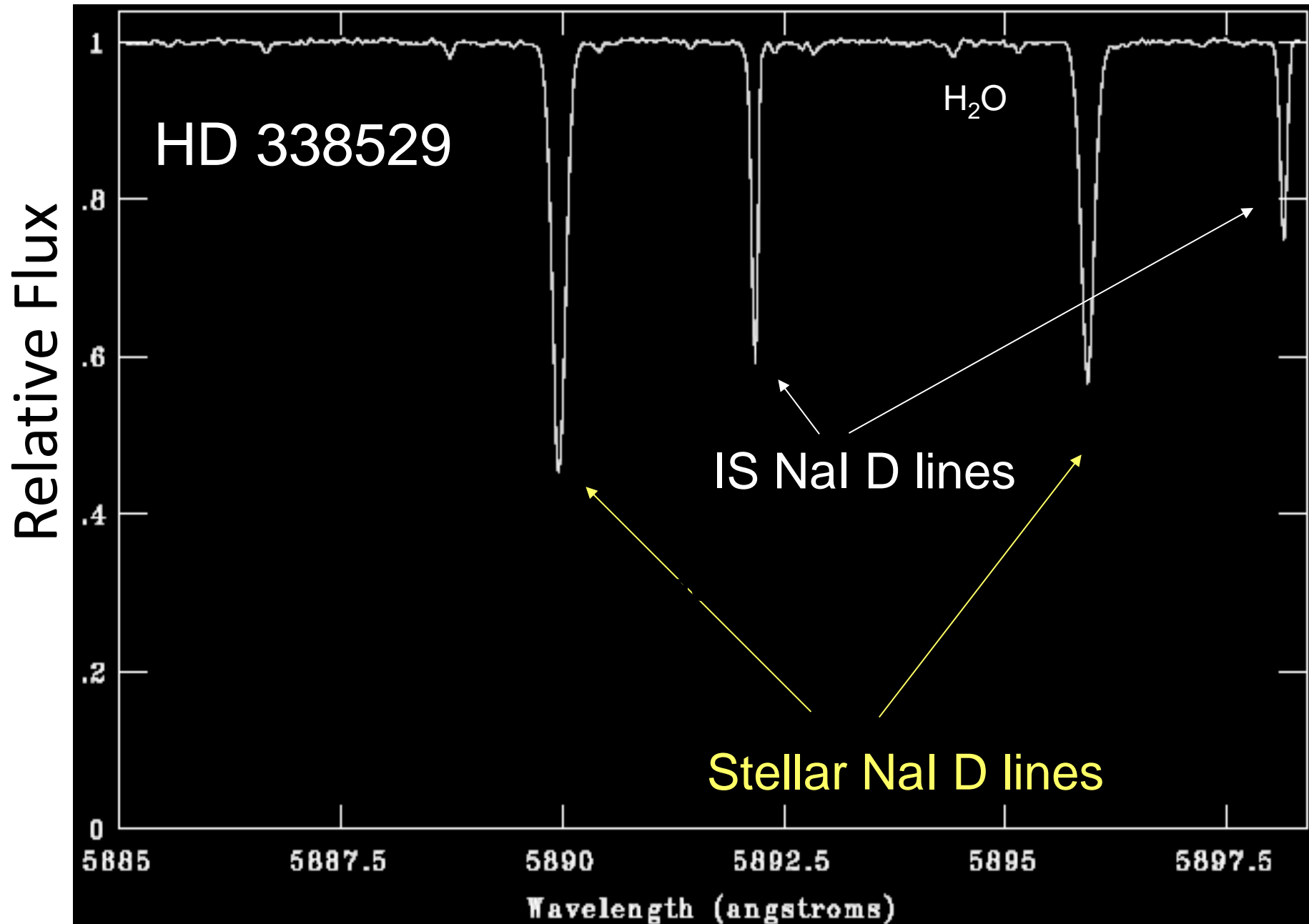
# Estrela sem linhas de absorção do MIS

$$E(B-V) = 0.000 \pm 0.001 \text{ mag}$$



# Estrela com linhas de absorção do MIS

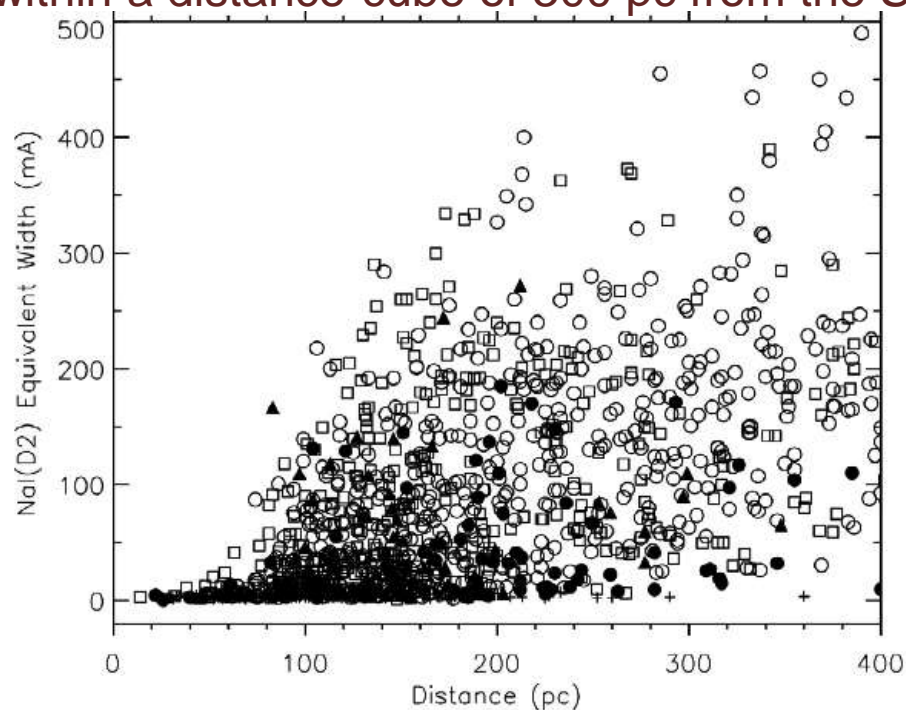
$$E(B-V) = 0.008 \pm 0.001 \text{ mag}$$



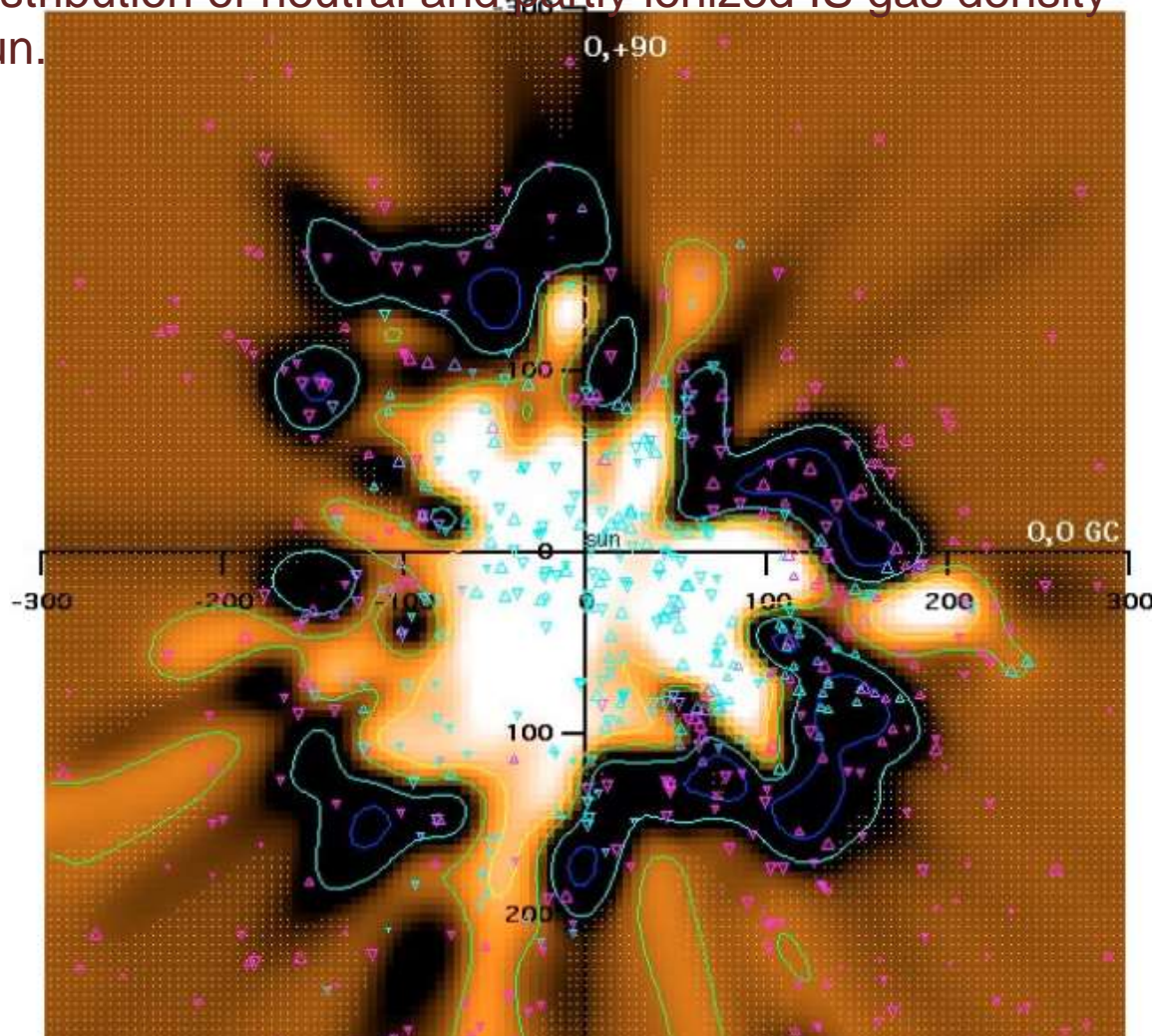


# New 3D gas density maps of NaI and CaII interstellar absorption within 300 pc<sup>★,★★</sup>

Catalog of absorptions towards 1857 early-type stars within 800 pc of the Sun. Using these data we determine the approximate 3-D spatial distribution of neutral and partly ionized IS gas density within a distance-cube of 300 pc from the Sun.



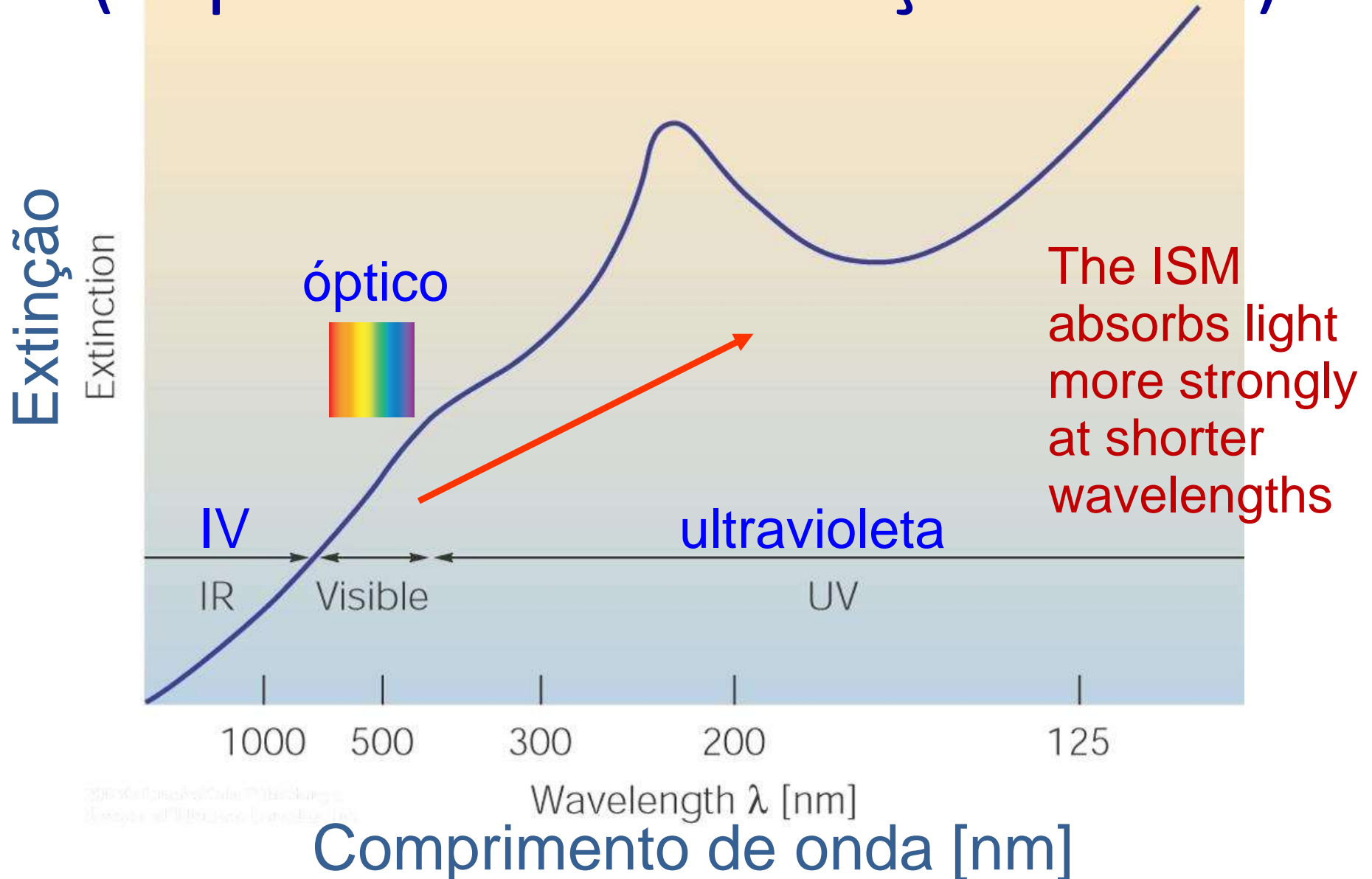
**Fig. 7.** Plot of the equivalent width (mÅ) of the interstellar NaI D2-line for stars with distances <400 pc. Filled triangles are for sight-lines with galactic latitude  $b > +45^\circ$ , open squares for sight-lines with  $b = 0$  to  $45^\circ$ , open circles for sight-lines with  $b = 0$  to  $-45^\circ$  and filled circles for sight-lines with  $b < -45^\circ$ . Crosses are upper limit values. Note the sharp increase in the level of NaI absorption at  $\sim 80$  pc, which is due to the neutral wall to the Local Cavity.



**Fig. 12.** Plot of 3D spatial distribution of interstellar NaI absorption within 300 pc of the Sun as viewed in the galactic plane projection. Triangles represent the sight-line positions of stars used to produce the map, with the size of the triangle being proportional to the derived NaI column density. Stars plotted with vertex upwards are located above the galactic plane, vertex down are below the plane. White to dark shading represents low to high values of the NaI volume density ( $n_{\text{NaI}}$ ). The corresponding iso-contours (yellow, green, turquoise and blue) for  $\log n_{\text{NaI}} = -9.5, -9.1, -8.5$  and  $-7.8 \text{ cm}^{-3}$  are also shown. Regions with a matrix of dots represent areas of uncertain neutral gas density measurement.

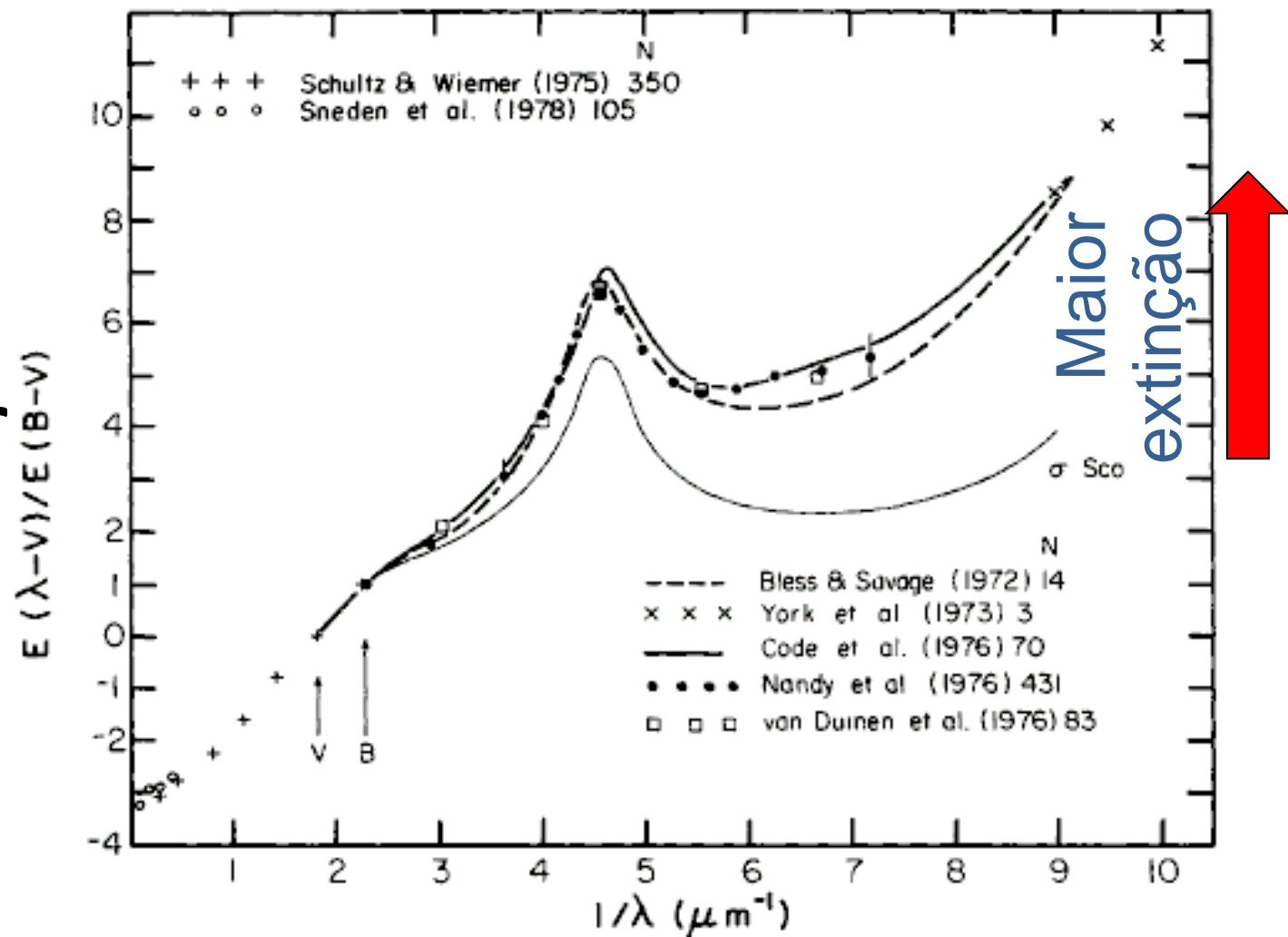
# Curva de extinção interestelar

(dependência da extinção com  $\lambda$ )





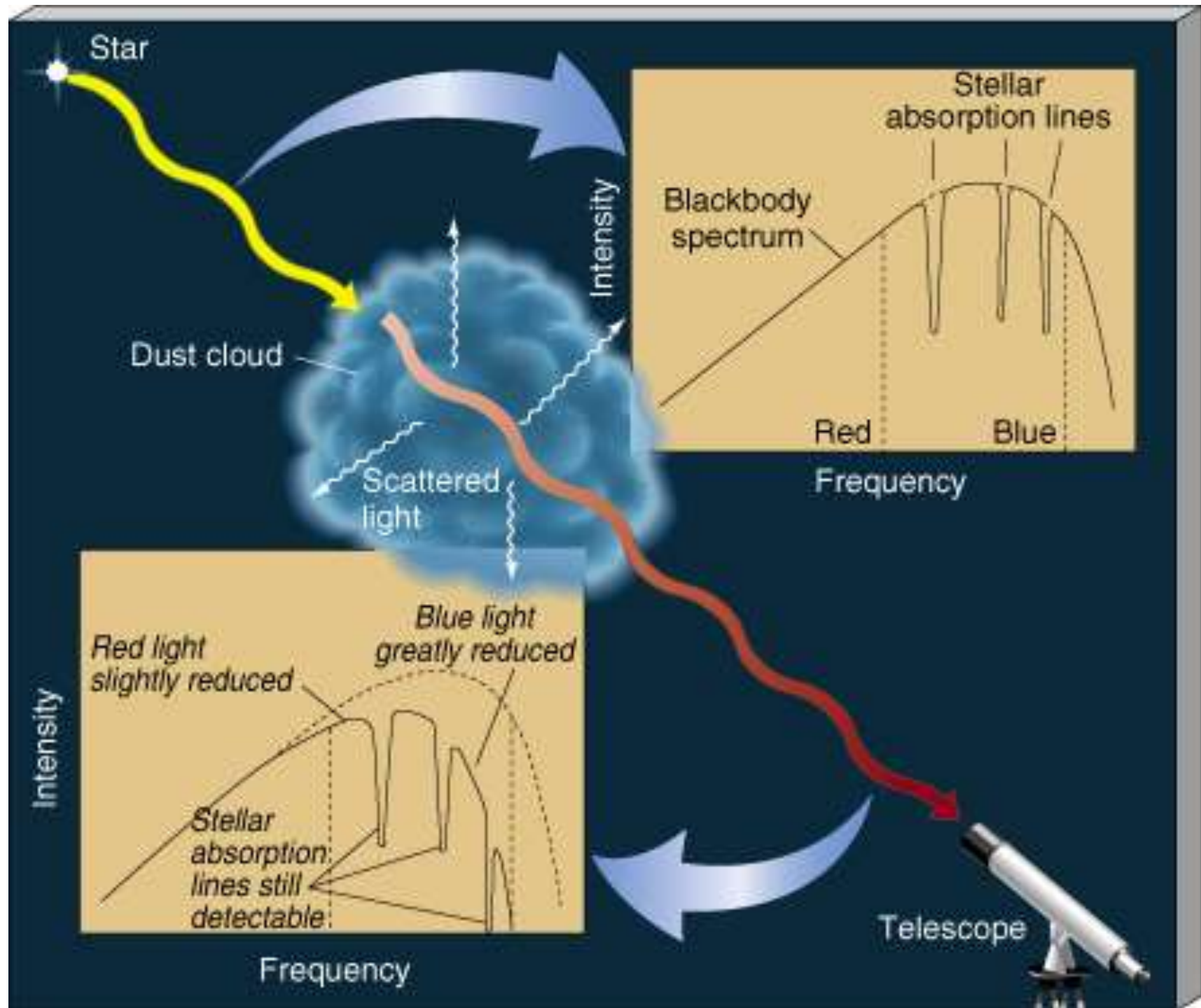
# Curva de Extinção Interestelar



Savage & Mathis  
1979, ARA&A 17, 73

Figure 1 Average normalized interstellar extinction is plotted versus  $1/\lambda$  in  $\mu m^{-1}$ .  $E(\lambda-V)$  refers to the extinction in magnitudes between a wavelength  $\lambda$  and the photoelectric  $V$  band. The references for the various curves are provided along with an indication of how many stars were used to derive each average curve. One abnormal ultraviolet curve for  $\sigma$  Sco from Bless & Savage (1972) is also shown. The average curves plotted can be converted to total normalized extinction,  $A_{\lambda}/E(B-V)$ , by adding  $R = 3.1$  to the quantity plotted. Note that the normalization to  $E(B-V) = 1$  implies a corresponding hydrogen column density of  $N(HI+H_2) = 5.8 \times 10^{21}$  atoms  $cm^{-2}$  (see Section 2). The error bars on two of the TD-1 points (Nandy et al. 1976) give an indication of the maximum observed variation in the average extinction curves derived for different galactic regions.

# Efeitos da extinção pela poeira interestelar





# Extinção Interestelar $A_x$

$$A_x \equiv m_x - m_{x0} \Rightarrow m_{x0} = m_x - A_x$$

➤  $A_x$ : extinção

➤  $m_x$ : magnitude observada

➤  $m_{x0}$ : magnitude intrínseca (o que seria observado em ausência de poeira IS)

**Exemplo:  $A_v = V - V_0 \Rightarrow V_0 = V - A_v$**

# Exemplo

$$A_x \equiv m_x - m_{x0} \Rightarrow m_{x0} = m_x - A_x$$

➤  $A_V = 1,5 \text{ mag}$

➤  $V = 11,6 \text{ mag}$

➤  $V_0 = V - A_V = 10,1$  (magnitude intrínseca, ou seja, a que seria observada em ausência de poeira IS)



# Excesso de cor $E(X-Y)$

$$E(X-Y) \equiv (m_X - m_Y) - (m_{X_0} - m_{Y_0})$$

- $E(X-Y)$ : excesso de cor
- $m_X - m_Y$ : cor observada
- $m_{X_0} - m_{Y_0}$ : cor intrínseca

**Exemplo:  $E(B-V) = (B-V) - (B_0-V_0)$**

**$\Rightarrow (B-V)_0 = (B-V) - E(B-V)$**

# Excesso de cor $E(X-Y)$

$$E(X-Y) \equiv (m_X - m_Y) - (m_{X0} - m_{Y0})$$

$$E(X-Y) \equiv (m_X - m_{X0}) - (m_Y - m_{Y0})$$

$$E(X-Y) \equiv A_X - A_Y$$

**Exemplo:  $E(B-V) = A_B - A_V$**



# Exemplo

$$A_B = 1,05 \text{ mag}, A_V = 0,90 \text{ mag}$$

$V = 10,1$  e  $B = 10,9$ , qual o valor de  $(B-V)_0$  ?

$$E(B-V) = 1,05 - 0,90 = 0,15$$

$$B-V = 10,9 - 10,1 = 0,80$$

$$(B-V)_0 = (B-V) - E(B-V) = 0,80 - 0,15$$

$$(B-V)_0 = 0,65$$

# Exemplo

$$E(B-V) = 0,15$$

$B-V = 0,80$  e  $V-R = 0,5$ , qual o valor de  $(V-R)_0$  ?

$$(V-R)_0 = (V-R) - E(V-R) = \dots$$



**Table 2** An average interstellar extinction curve

	$\lambda(\mu\text{m})$	$\lambda^{-1}(\mu\text{m}^{-1})$	$E(\lambda-V)/E(B-V)$	$A_\lambda/E(B-V)$
	$\infty$	0	-3.10	0.00
<i>L</i>	3.4	0.29	-2.94	0.16
<i>K</i>	2.2	0.45	-2.72	0.38
<i>J</i>	1.25	0.80	-2.23	0.87
<i>I</i>	0.90	1.11	-1.60	1.50
<i>R</i>	0.70	1.43	-0.78	2.32
<i>V</i>	0.55	1.82	0	3.10
<i>B</i>	0.44	2.27	1.00	4.10
	0.40	2.50	1.30	4.40
	0.344	2.91	1.80	4.90
	0.274	3.65	3.10	6.20
	0.250	4.00	4.19	7.29
	0.240	4.17	4.90	8.00
	0.230	4.35	5.77	8.87

Savage & Mathis 1979,  
ARA&A 17, 73

**Careful: this is for  
R, I in the Johnson (J)  
system. Now most  
people use R, I in the  
Cousin (C) system.**

- $E(V-R)^J = 0.78 E(B-V)$      $E(V-R)^C = 0.60 E(B-V)$
- $E(V-I)^J = 1.60 E(B-V)$      $E(V-I)^C = 1.25 E(B-V)$
- $E(V-K)^J = 2.72 E(B-V)$
- $E(J-K)^J = 0.22 E(B-V)$
- $E(b-y) = 0.73 E(B-V)$
- $E(m_1) = -0.33E(b-y) = -0.24 E(B-V)$
- $E(c_1) = 0.17 E(b-y) = 0.12 E(B-V)$

# Valores de $A_V$ , $E(B-V)$

$$R = \frac{A_V}{E(B-V)} \approx 3,1$$

- $d < 80-100$  pc (0.1 kpc)  $\Rightarrow E(B-V) \sim 0$
- $E(B-V) \approx 0.53 d$  (kpc)
- $A_V \approx 1,6 d$  (kpc) magnitudes

Bond (1980, ApJS 44,517):

- $b$  dentro de  $30^\circ$  polo norte Gal.:  $E(B-V) = 0.00$
- $b$  dentro de  $30^\circ$  polo sur Gal.:  $E(B-V) = 0.03$
- $|b| < 60^\circ$  do plano:

$$E(B-V) = 0.03 \csc b [1 - \exp(-0.008 d(\text{pc}) \sin|b|)]$$



# EXTINCT

Hakkila et al. 1997, AJ 114, 2043

$A_V$ : EXTINCT.FOR

$l, b, d(\text{kpc})$

[ftp.mankato.msus.edu/pub/astro](ftp://mankato.msus.edu/pub/astro)

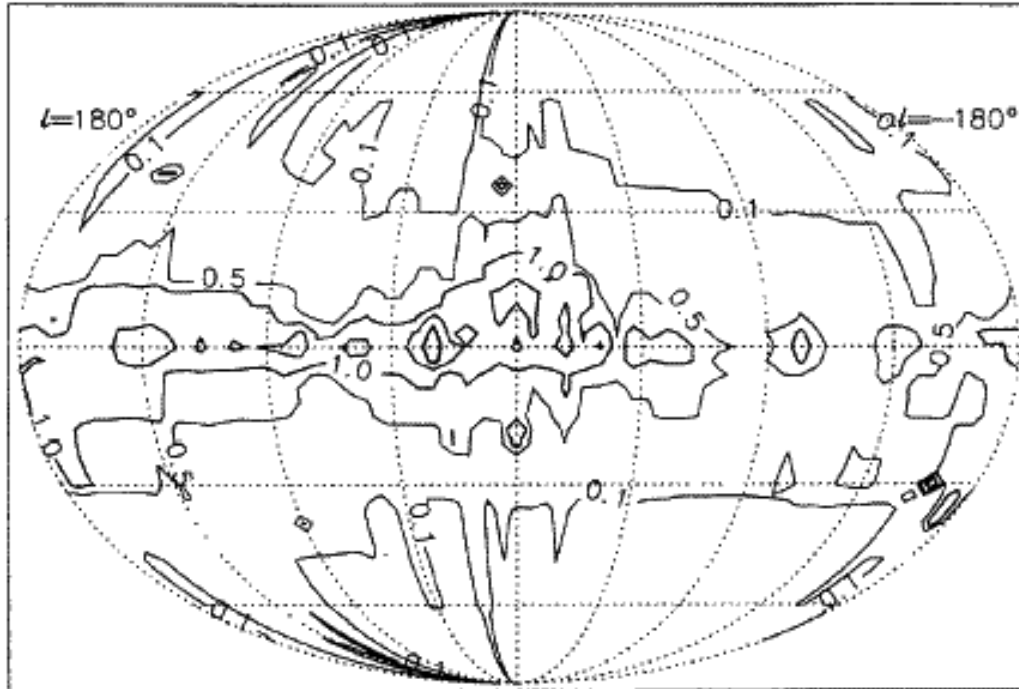


FIG. 11. Total visual extinction  $A_V$  (mag) in Galactic coordinates to a distance of 1 kpc as obtained from combining the results of all studies. When available, extinction from individual clouds identified in the high-latitude study is used. Otherwise, the results represent an average of available sub-routines weighted equally. Contours in this plot are 0.1, 0.5, 1.0, 2.0, and 3.0 mag.

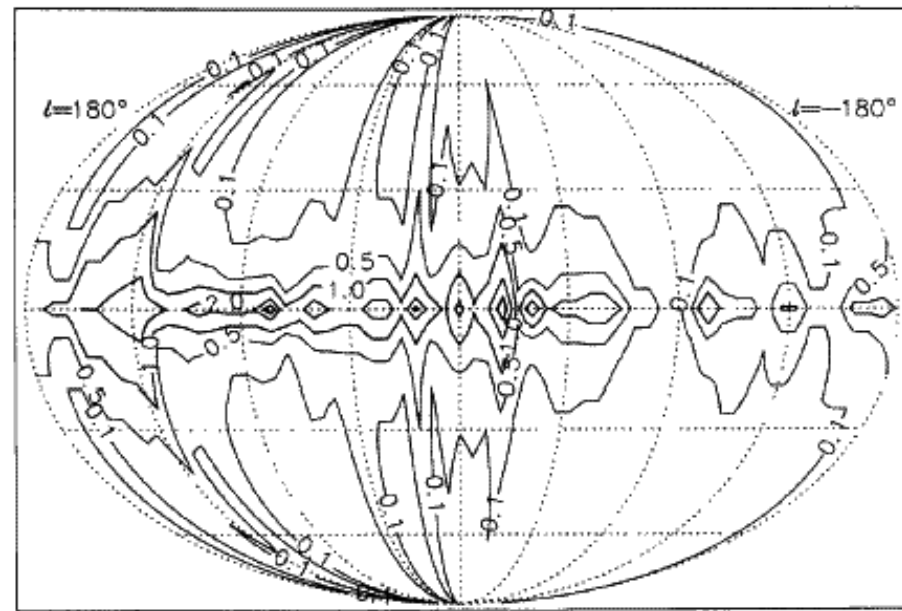


FIG. 2. Total visual extinction  $A_V$  (magnitudes) in Galactic coordinates to a distance of 1 kpc as obtained from the FitzGerald (1968) study. Plot contours are 0.1, 0.5, 1.0, 2.0, and 3.0 mag.

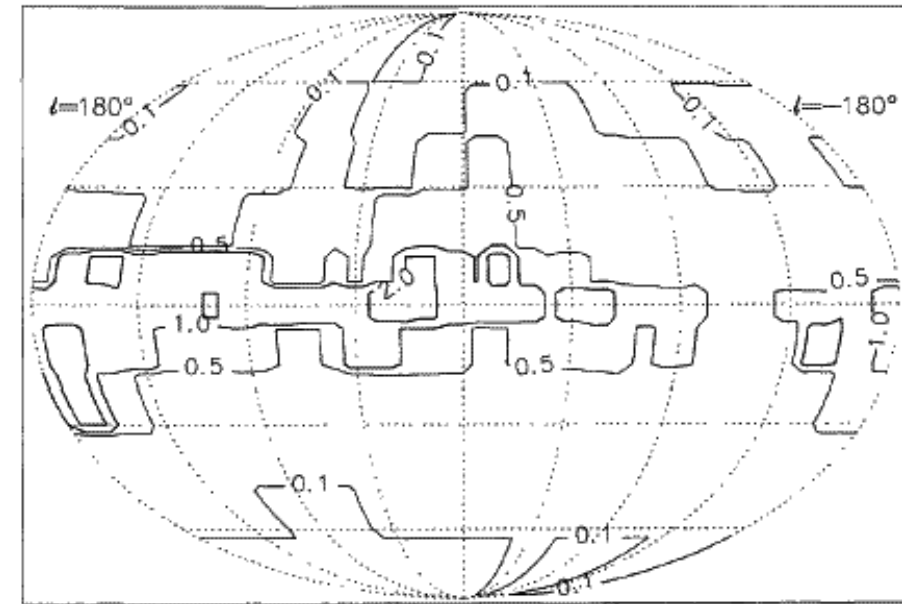
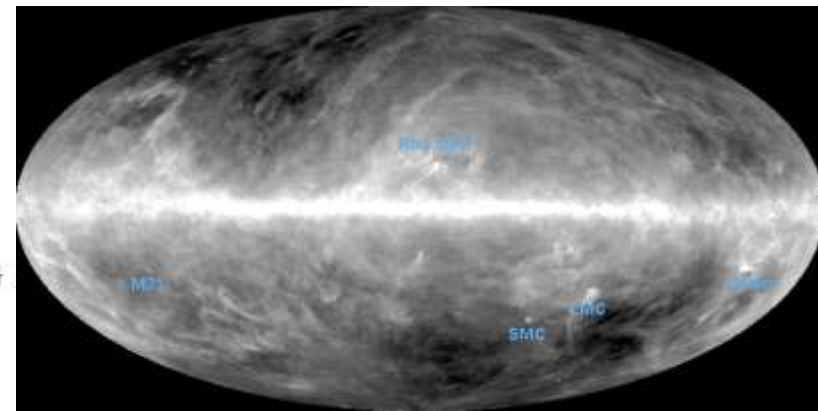


FIG. 7. Total visual extinction  $A_V$  (magnitudes) in Galactic coordinates to a distance of 1 kpc as obtained from the Arenou *et al.* (1992) study. Plot contours are 0.1, 0.5, 1.0, 2.0, and 3.0 mag.

# Schlegel et al. maps



THE ASTROPHYSICAL JOURNAL, 500:525–553, 1998 June 20  
MAPS OF DUST INFRARED EMISSION FOR USE IN ESTIMATION OF REDDENING  
COSMIC MICROWAVE BACKGROUND RADIATION FOREGROUNDS

DAVID J. SCHLEGEL

University of Durham, Department of Physics, South Road, Durham DH1 3LE, UK; D.J.Schlegel@durham.ac.uk

AND

DOUGLAS P. FINKBEINER AND MARC DAVIS

<http://astro.berkeley.edu/~marc/dust/>

Melendez et al. 2006, ApJ, 642, 1082

We adopted the following correction for the S98 maps:

<http://ned.ipac.caltech.edu/forms/calculator.html>

$$E_{B-V}^{S98c} = 0.9E_{B-V}^{S98} - 0.01$$

## NASA/IPAC EXTRAGALACTIC DATABASE

### Coordinate Transformation & Galactic Extinction Calculator

[Help](#) | [Comment](#) | [NED Home](#)

#### Input parameters:

System:  Equinox:

Observation epoch:

RA or Longitude:

DEC or Latitude:

PA (East of North):

#### Output Parameters:

System:  Equinox:



# Schlegel et al. maps

THE ASTROPHYSICAL JOURNAL, 500:525–553, 1998 June 20  
 MAPS OF DUST INFRARED EMISSION FOR USE IN ESTIMATION OF REDDENING AND  
 COSMIC MICROWAVE BACKGROUND RADIATION FOREGROUNDS

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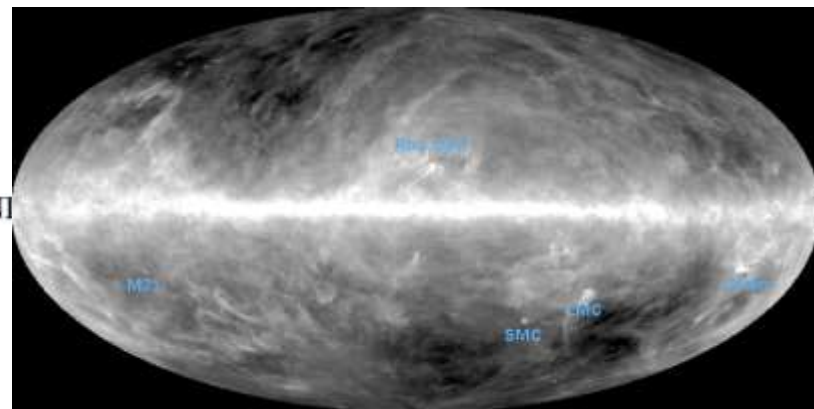


TABLE 6

RELATIVE EXTINCTION FOR SELECTED BANDPASSES

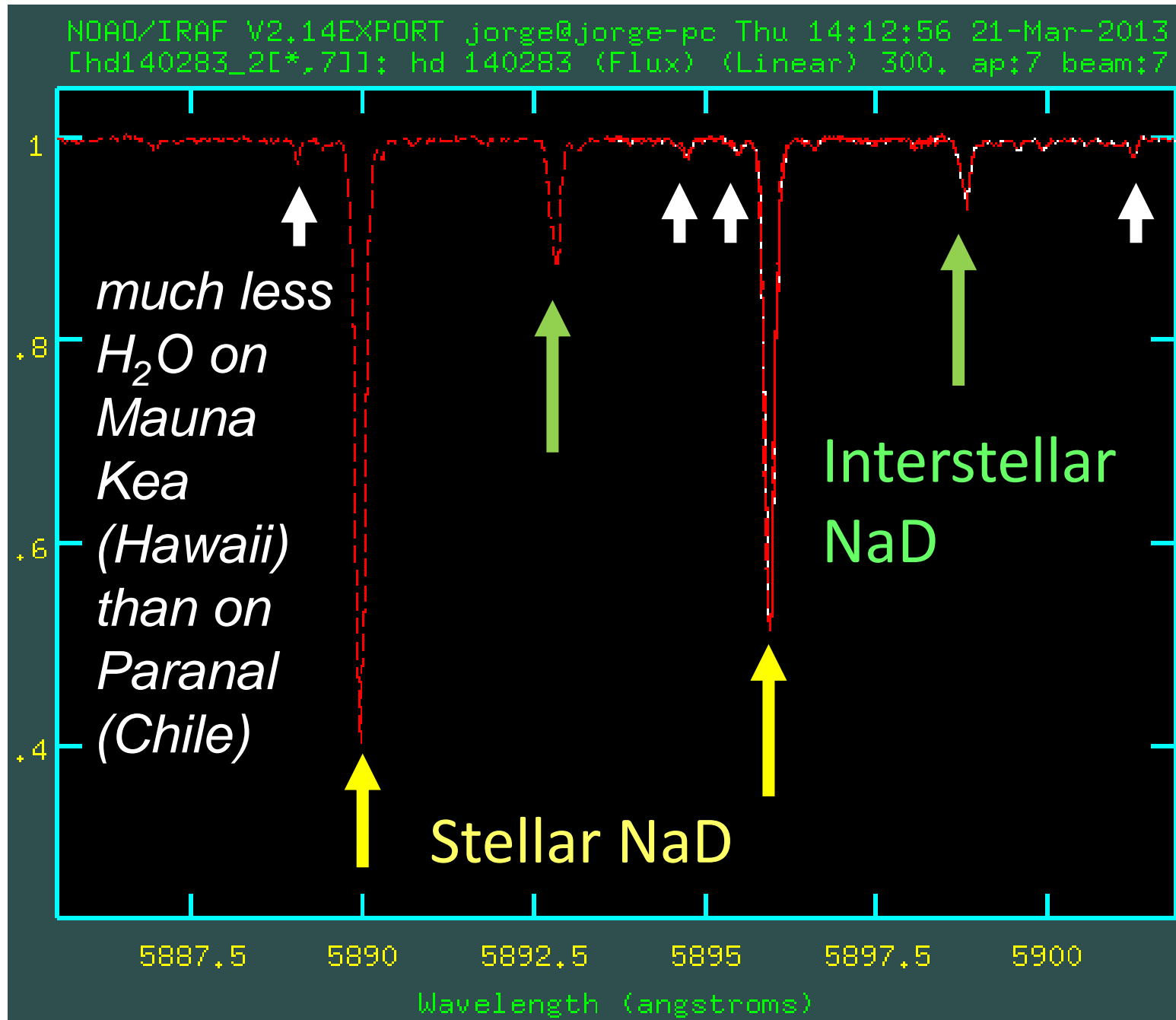
Filter	$\lambda_{\text{eff}}$ (Å)	$A/A(V)$	$A/E(B-V)$	Filter	$\lambda_{\text{eff}}$ Å	$A/A(V)$	$A/E(B-V)$
Landolt <i>U</i> .....	3372	1.664	5.434	Strömgen <i>u</i> .....	3502	1.602	5.231
Landolt <i>B</i> .....	4404	1.321	4.315	Strömgen <i>b</i> .....	4676	1.240	4.049
Landolt <i>V</i> .....	5428	1.015	3.315	Strömgen <i>v</i> .....	4127	1.394	4.552
Landolt <i>R</i> .....	6509	0.819	2.673	Strömgen $\beta$ .....	4861	1.182	3.858
Landolt <i>I</i> .....	8090	0.594	1.940	Strömgen <i>y</i> .....	5479	1.004	3.277
CTIO <i>U</i> .....	3683	1.521	4.968	Sloan <i>u'</i> .....	3546	1.579	5.155
CTIO <i>B</i> .....	4393	1.324	4.325	Sloan <i>g'</i> .....	4925	1.161	3.793
CTIO <i>V</i> .....	5519	0.992	3.240	Sloan <i>r'</i> .....	6335	0.843	2.751
CTIO <i>R</i> .....	6602	0.807	2.634	Sloan <i>i'</i> .....	7799	0.639	2.086
CTIO <i>I</i> .....	8046	0.601	1.962	Sloan <i>z'</i> .....	9294	0.453	1.479
UKIRT <i>J</i> .....	12660	0.276	0.902	WFPC2 F300W .....	3047	1.791	5.849
UKIRT <i>H</i> .....	16732	0.176	0.576	WFPC2 F450W .....	4711	1.229	4.015
UKIRT <i>K</i> .....	22152	0.112	0.367	WFPC2 F555W .....	5498	0.996	3.252
UKIRT <i>L</i> .....	38079	0.047	0.153	WFPC2 F606W .....	6042	0.885	2.889
Gunn <i>g</i> .....	5244	1.065	3.476	WFPC2 F702W .....	7068	0.746	2.435
Gunn <i>r</i> .....	6707	0.793	2.590	WFPC2 F814W .....	8066	0.597	1.948
Gunn <i>i</i> .....	7985	0.610	1.991	DSS-II <i>g</i> .....	4814	1.197	3.907
Gunn <i>z</i> .....	9055	0.472	1.540	DSS-II <i>r</i> .....	6571	0.811	2.649
Spinrad $R_S$ .....	6993	0.755	2.467	DSS-II <i>i</i> .....	8183	0.580	1.893
APM $b_J$ .....	4690	1.236	4.035				

R, I are  
 both in  
 the  
 Cousin  
 system



NOTE.—Magnitudes of extinction evaluated in different passbands using the  $R_V = 3.1$  extinction laws of Cardelli et al. 1989 and O'Donnell 1994. The final column normalizes the extinction to photoelectric measurements of  $E(B-V)$ .

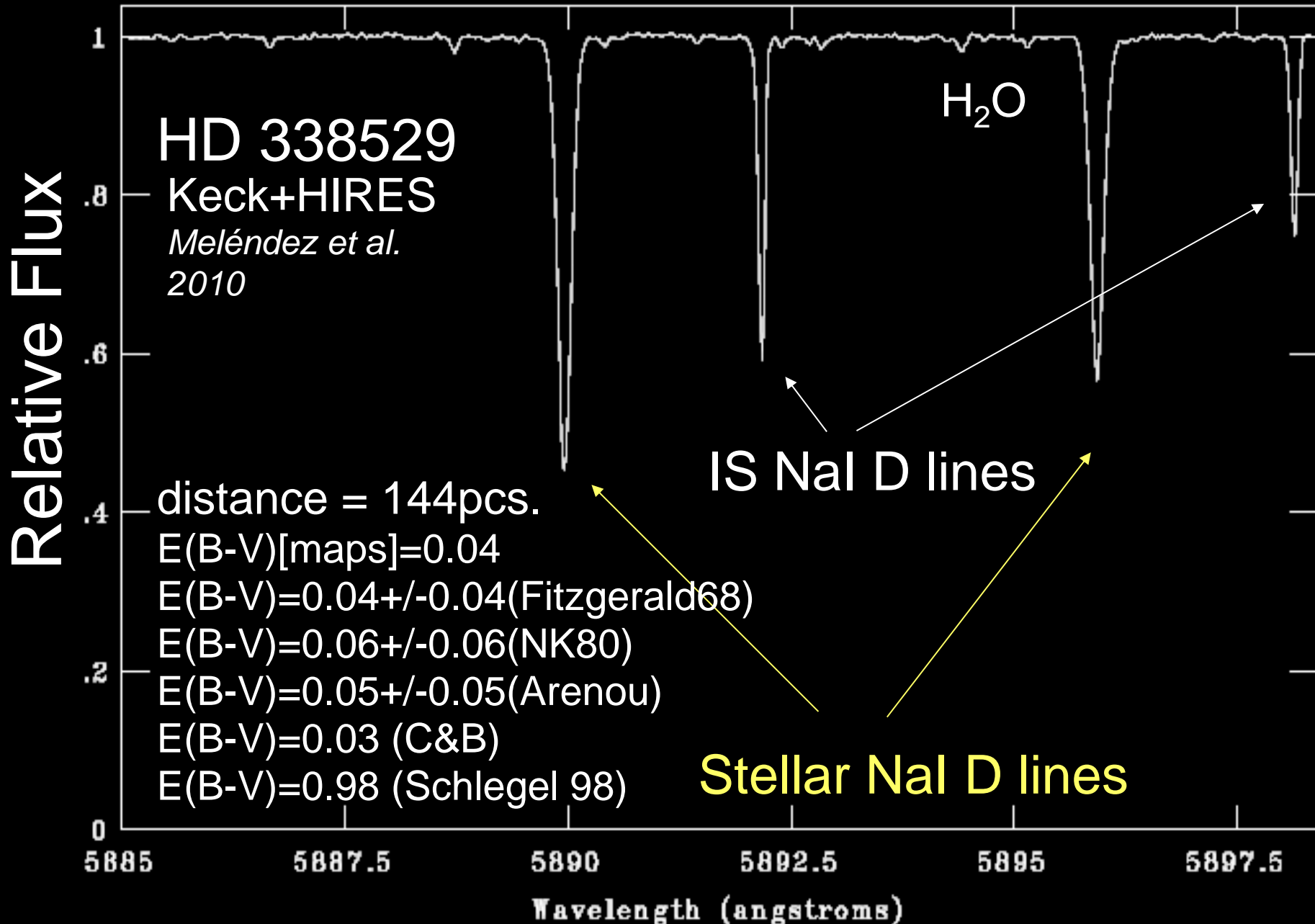
# Keck (4.2km) spectrum of HD140283





# E(B-V): using NaD lines

$$E(B-V) = 0.008 \pm 0.001 \text{ mag}$$



# Como calcular $E(B-V)$ ?

- Longe do plano da Galáxia (latitudes  $b < -20^\circ$  e latitudes  $b > +20^\circ$ ) o mais simples é utilizar os mapas do Schegel et al. (1998)

<http://ned.ipac.caltech.edu/forms/calculator.html>

- Para latitudes próximas ao plano, podem usar a receita apresentada no slide a seguir



# How to deal with IS reddening : maps

THE ASTROPHYSICAL JOURNAL, 642:1082–1097, 2006 May 10

JORGE MELÉNDEZ<sup>1</sup> NATALIYA G. SHCHUKINA AND IRINA E. VASILJEVA IVÁN RAMÍREZ<sup>1</sup>

1.  $E_{B-V}^{\text{maps}} = 0.0$  for stars within 75 pc.
2. For stars with  $75 \text{ pc} < d \leq 100 \text{ pc}$ ,  $E_{B-V}^{\text{maps}} = (E_{B-V}^{H97} + (E_{B-V}^{B80} + E_{B-V}^{C98})/2 + 2 \times 0.0)/4$ . The factor  $2 \times 0.0$  considers a 50% chance of zero reddening.
3. If a star has  $d > 100 \text{ pc}$  and  $|b| > 45^\circ$ ,  $E_{B-V}^{\text{maps}} = (nE_{B-V}^{H97} + mE_{B-V}^{S98c})/(n + m)$ , where  $n$  is the square root of the number of maps used in H97 and  $m = (d + 1.5)(\sin |b|)^{1.5}$ , with  $d$  in kpc. This empirical parameterization gives a high weight to the S98 map for high-latitude and/or distant objects, and a weight essentially zero for low-latitude stars.
4. Stars with  $d > 100 \text{ pc}$  and  $|b| \leq 45^\circ$ ,  $E_{B-V}^{\text{maps}} = (nE_{B-V}^{H97} + mE_{B-V}^{S98c} + (E_{B-V}^{B80} + E_{B-V}^{C98})/2)/(n + m + 1)$ . The weights  $n$  and  $m$  are equal to the previous case, except that  $m = 0$  if  $E_{B-V}^{S98c} > 2E_{B-V}^{H97}$  (in some cases this restriction was relaxed, especially for very distant objects with  $|b| > 30^\circ$ ).
5. If after applying the above criteria  $E_{B-V}^{\text{maps}} > E_{B-V}^{S98c}$ , then we adopted  $E_{B-V}^{\text{maps}} = E_{B-V}^{S98c}$ .

# How to deal with IS reddening : Na D

A&A 513, A35 (2010)

A. Alves-Brito<sup>1,2</sup>, J. Meléndez<sup>3</sup>, M. Asplund<sup>4</sup>, I. Ramírez<sup>4</sup>, and D. Yong<sup>5</sup>

tion lines were used. The  $E(B - V)$  values based on the D lines were obtained as follows. In the optical thin case the relation between column density  $N$  (units  $\text{cm}^{-2}$ ) and equivalent width  $EW$  (units  $\text{m}\text{\AA}$ ) is

$$N = 1.13 \times 10^{17} EW / (f \lambda^2) \quad (1)$$

The  $N(\text{Na I})$  density was transformed to  $N(\text{H})$  with the relation found by Ferlet et al. (1985):

$$\log N(\text{HI} + \text{H}_2) = (\log N(\text{NaI}) + 9.09) / 1.04, \quad (2)$$

where both  $N(\text{Na I})$  and  $N(\text{H})$  are in  $\text{cm}^{-2}$ . Finally,  $E(B - V)$  was computed from the total hydrogen density (Bohlin et al. 1978)

$$E(B - V) = N(\text{HI} + \text{H}_2) / 5.8 \times 10^{21}, \quad (3)$$

where  $N(\text{H})$  is in  $\text{cm}^{-2}$  and  $E(B - V)$  in magnitudes. Although this relation seems not well established for  $E(B - V) < 0.1$ , Ramirez et al. (2006) have shown it to be very accurate for a  $E(B - V) = 0.01$  star.



# Exemplo

Valores observados:  $V = 9,831$ ;  $B-V = 0,750$ ;  $V-R = 0,464$

Se  $E(B-V) = 0,10$ , quais os valores corrigidos da extinção interestelar para a magnitude  $V$  e as cores  $B-V$  e  $V-R$ ?

Usar a tabela de Schlegel (slide 42).

Adotando  $A_V / E(B-V) = 3,315 \rightarrow A_V = 0,331$

$$V_0 = V - A_V = \mathbf{9,500}$$

$$(B-V)_0 = (B-V) - E(B-V) = \mathbf{0,650}$$

$A_V / E(B-V) = 3,315$ ,  $A_R / E(B-V) = 2,673$ , ou seja  $A_V - A_R = 0,642 E(B-V)$ . Como  $E(V-R) = A_V - A_R \rightarrow E(V-R) = 0,642 E(B-V) = 0,064$

*Nota: no slide 38 já tínhamos sugerido que  $E(V-R) \sim 0,6 E(B-V)$ , mas agora verificamos usando a tabela do Schlegel que de fato esse é o caso.*

$$(V-R)_0 = (V-R) - E(V-R) = \mathbf{0,400}$$